

Effects of Exit Geometry on Turbulent Mixing in Supersonic Flows



by

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Presentation at

Tokyo University December 21, 2015





The highlights of this presentation are:

- Turbulent Mixing and its Relevance to Volcanic Eruptions.
- Studies on Supersonic Nozzles of Complex Geometry
- Near Field flow using PLIF and 3D-CFD
- Far Field flow using Hot-Wire Anemometry
- Definition of entrainment from hot wire anemometry profiles.
- Implications of these studies to volcanic eruptions.



Turbulent Mixing in Volcanic Plumes



Huge Range of Turbulent Mixing scales in a Volcanic Plume. (http://www.geo.mtu.edu/volcanoes/hazards/primer/images/volcimages/sthelenserup.jpg) Turbulent Entrainment and Mixing between the ejected material (volcanic gas and hot ash (solid)) from a volcanic eruption and the ambient air, is crucial in the dynamics and development of the plume and hence the kind of disaster it can cause (Suzuki and Koyaguchi, Earth Diant Search 2012 June 4 Farth Similar

Earth Planets Space, 2013, Journal of Earth Simulator,

2007).

- The kind of volcanic plume completely dependent on :
 - Rate of density change with height.
 - Entrainment and Mixing with the ambient air





Schematic of a Plinian Eruption

 Large entrainment and mixing between hot pyroclast and air causes global density of the plume to fall, buoyancy gives rise to very high plinian eruption.



Schematic of a Fountain type of Eruption with Pyroclatic flow. (Greg & Kenneth, J. Geophysical Research, 1989)

Low entrainment does not decrease the global density and hence the eruption column collapses under gravity causing pyroclastic flow along the ground.



Explosive Volcanic Eruption as A Supersonic Free Jet



Study on the effect of geometry and flow condition on jet features (Hatanaka & Saito, Shock Waves, 2012)



 High overpressures within the volcano causes a supersonic jet to develop.(Greg & Kenneth, 1989; Ogden et.al. J. Geophysical Research, 2008)



- Effect of compressibility at high Mach numbers decreases mixing rate
- Nozzle exit geometry influences the mixing rate to a great extent due to production of streamwise vortices (Rao & Jagadeesh, ATE, 2015).

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Supersonic Turbulent Jet



- Based on flow features observed, the supersonic jet plume can be divided into the near field and the far field.
- The near field is characterized by presence of shock structures, contains a supersonic core.
- The far field is largely subsonic, distinct core is lost and highly turbulent.
- Near Field flow (<6D) is investigated using PLIF technique, Pitot measurements.
- Far field (>40D) flow using Hot Wire Anemometry.



Nozzles with complex shaped exits



(a) TypeA: Conical Nozzle



(c) Type C: Serrated Nozzle

Throat Dia 5 [mm]

(b) Type B: Beveled Conical Nozzle



4 different kinds of supersonic nozzles

Near Field Studies

室蘭工業大学





- Experiments conducted at NPR=6.0
- Acetone PLIF @ 10 Hz, using Hamamatsu ICCD in streamwise and cross-sectional planes.
- CFD studies using FASTAR(JAXA), 8 million cells in the mesh, Spallart Almaras turbulence model.

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Image Processing of PLIF images

- Histogram based image decomposition of PLIF images.
- Helps to identify mixing layer growth.
- Steady flow of about 2 secs.





- Type C and Type D nozzle show maximum difference of flow.
- Type D nozzle shows the highest increase of mixing rate.
- Exit flow star shaped in Type C, 6-lobed shape in Type D
- By about 8D the nozzles regain circular shapes



Nozzle Type	: Type A		Type C	Type D	
Growth rate dW/dZ	0.072 0.099		0.159	0.308	
% Increase	-	138%	222%	430%	

Table of average growth rate of jet width vs Z

Nozzle Type	Type A	Type B	Type C	Type D				
Z=15 mm								
Area (A)	2.94×10 ⁴	2.94×10 ⁴ 3.93×10 ⁴		5.85×10 ⁴				
A/A _{TypeA}	1.00	1.34	1.61	1.99				
Z=40 mm								
Area (A)	5.40×10 ⁴	4.60×10 ⁴	6.04×10 ⁴	1.24×10 ⁵				
A/A _{TypeA}	1.00	0.85	1.12	2.29				

Table of cross sectional areas (in pixel units) evaluated from

cross-sectional PLIF images for the four nozzles.







- Pitot pressures and their profiles from experiment and CFD are in good agreement.
- The density contours show flow features that are similar to the observations from PLIF.



Vorticity and its Production



Vorticity contours near the exit of the nozzle

- Streamwise vorticity high in Type C and Type D nozzles.
- Wide-spread vortices in Type D, clustered vortices in Type C.
- Pressure gradient across the lobes from throat to exit causes formation of large vortices.
- Shape of the nozzle exit plays an important role in determining entrainment and mixing rate near the nozzle exit.

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- The hot-wire anemometry is used for accurate velocity measurement with high frequency response.
- Heat transfer across a heated thin wire (\approx 5 μ m) is related to the velocity.
- A fourth order polynomial fit relates voltage across the wire to velocity.



- In the far field centerline velocity decays linearly
- The velocity profile is gaussian and self-similar in the far-field
- These observations match previous studies of Hussien et al. JFM, 1994.



- Hot wire anemometry experiments are conducted at X≥40D
- The slope of linear profiles indicate the differences in centerline velocity decay
- Type D shows the maximum decay rate, then Type C. Type A and Type B are similar in magnitude.



- Velocity profiles in the far field are not very different
- Type B shows the effects of slight bending by producing asymmetry of velocity profiles.
- Velocity profiles are very nearly similar in the far field. Velocity decay rate is affected by geometry and near field structure.



Knowing the velocity profiles the entrainment can be defined based on mass conservation

$$E = \lim_{r \to \infty} (-2\pi r V) = \frac{\mathrm{d}}{\mathrm{d}x} \left[2\pi \int_0^\infty Ur \,\mathrm{d}r \right] = 2\pi B(M_0)^{\frac{1}{2}} \int_0^\infty \left[\frac{U}{U_c} \right] \eta \,\mathrm{d}\eta.$$

The entrainment ratio is then defined as :

$$b = I_1 x / (I_2)^{\frac{1}{2}},$$

$$W = (I_2/I_1) B(M_0)^{\frac{1}{2}}/x,$$

$$E_2 = I_1 B(M_0)^{\frac{1}{2}},$$

$$b^2 W = 2 \int_0^\infty Ur \, dr,$$

$$I_1 = 2 \int_0^\infty \frac{U}{U_c} \eta \, d\eta,$$

$$U_c = (a + b\eta^2 + c\eta^4)e^{-A\eta^2}$$

$$I_2 = 2 \int_0^\infty (\frac{U}{U_c})^2 \eta \, d\eta,$$

$$I_1 = 2 \int_0^\infty \frac{U}{U_c} x \eta d\eta = \frac{a}{A} + \frac{b}{A^2} + \frac{2c}{A^3}$$

$$E' = \frac{d}{dx} \left(2 \int_0^\infty Ur \, dr \right),$$

$$\alpha = I_1/2(I_2)^{\frac{1}{2}},$$

$$I_2 = 2 \int_0^\infty (\frac{U}{U_c})^2 x \eta d\eta = \frac{a^2}{2A} + \frac{a^2}{2A^2} + \frac{b^2 + 2ac}{4A^3} + \frac{3bc}{4A^4} + \frac{3c^2}{4A^5}$$

 $\alpha = \frac{E'}{2bW},$



- For the fan jet case the entrainment ratio is 0.0718
- For the four different supersonic nozzles

TYPE	а	b	С	Α	I1	I2	a
A	1	I −4.51887	5694.78	148.273	0.010033	0.004444	0.07525
В	1	6.14092	1915.59	104.158	0.013557	0.006239	0.08582
B minus	1	-8.47814	7329.25	150.047	0.010627	0.004672	0.07774
С	1	l –10.776	7238.05	150.065	0.010469	0.004573	0.07740
D	1	-8.12222	9678.49	175.639	0.009003	0.003970	0.07144

Entrainment ratios are of similar orders.



- Turbulent Jet Entrainment is important in understanding the nature of volcanic jets.
- The effect of nozzle exit shape is studied on four different kinds of supersonic free jets.
- A very strong influence of nozzle exit shape is seen in the near field of the jet, where the complex nozzles show high rates of entrainment.
- Streamwise vorticity production is responsible for this phenomenon.
- In the far field, the rate of centerline velocity decay is affected by the nozzle exit shape.
- The velocity profiles, however, show similarity.
- The entrainment ratio evaluated from velocity profiles are about 0.08 in majority of the cases.
- Studies are being planned to include the effects of a dusty-gas in experiments and numerical simulations.



- Prof. Tsutomu Saito.
- Prof. Mitsutomo Hirota.
- Members of Propulsion Laboratory, Dept. Of Aerospace Engineering, Muroran Institute of Technology. Especially, Mr. Asano, Mr. Ikeda for their help in conducting experiments.
- Indian Institute of Science and Lab members of LHSR (Prof. G. Jagadeesh and Prof. K.P.J. Reddy.)
- Organizers for the opportunity to share my ideas.



Thank You

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December 21, 2015