

1 **Supplementary Material:**

2 **Surface wave tomography for the Pacific Ocean incorporating seafloor seismic**  
3 **observations and plate thermal evolution**

4 *T. Isse et al.*

5

6 **S1. Effects of data weighting and results of the checkerboard resolution tests**

7           This study used more seismic stations and events in the western Pacific than in  
8 the eastern Pacific Ocean, and, therefore, the ray paths were denser in the former. To  
9 rebalance the uneven ray distribution and to account for the relatively small number of  
10 phase speed measurements per BBOBS station (as the observation period for BBOBS  
11 data is typically  $\sim 1$  year), we weighted the Rayleigh wave and Love wave data for events  
12 with longitudes greater than  $190^\circ\text{E}$ , latitudes outside the range of  $50^\circ\text{N}$ – $40^\circ\text{S}$ , or data  
13 recorded by a BBOBS. We changed the factor from 1.0 to 3.0 and performed the  
14 checkerboard resolution tests (Figure S2). When we did not apply weight to the data, the  
15 checkerboard patterns were well recovered only in the western Pacific Ocean (Figure S2a  
16 and d). In the Rayleigh wave case, the well-recovered regions increased when factors of

17 2 and 3 were applied (Figure S2b and c). In the Love wave case, applying a factor of 3  
18 was necessary (Figure S2e and f). In our inversion method, we performed ray tracing so  
19 that a uniform recovered amplitude was preferable in the eastern and western parts of the  
20 Pacific Ocean. Figure S2c (Rayleigh wave, factor of 3) shows that the recovered  
21 amplitude was stronger in the eastern part than in the western part and that the regional  
22 difference of the recovered amplitude was larger than in the case of a factor of 2. In this  
23 study, we chose a factor of 2.0 in the Rayleigh wave data and 3.0 in the Love wave data.

24 We performed the checkerboard resolution tests to assess the horizontal  
25 resolution and the effects of applying different weighting schemes to the data. We  
26 calculated the synthetic path-averaged phase speed data from the input checkerboard  
27 models incorporating the finite frequency effect, and we subsequently inverted them for  
28 the phase speed maps.

29 Figure S2 shows an example of the results of  $8^\circ$  checkerboard resolution tests with  
30 different weights at a period of 83 s. In tests where the data were unweighted, the  
31 checkerboard pattern was recovered only in the western Pacific Ocean (Figure S2a and  
32 c). In tests where the Rayleigh wave and Love wave data were weighted as described in

33 the main text, the recovered amplitudes of the checkerboard patterns in the eastern Pacific  
34 Ocean were improved. The shapes of the checkerboard patterns were well recovered in  
35 the western and southeastern parts of the Pacific Ocean. Figure S3 shows the results of  
36 the checkerboard resolution tests for the fundamental-mode Love and Rayleigh waves at  
37 a period of 83 s with cell sizes of  $6^\circ$  to  $16^\circ$ . Checkerboard patterns were recovered in the  
38 entire Pacific Ocean when the cell sizes were larger than  $14^\circ$  and  $18^\circ$ , and in the western  
39 Pacific Ocean at cell sizes of  $6^\circ$  and  $10^\circ$  for the Rayleigh waves and Love waves,  
40 respectively. In the present study, the lateral resolution of the isotropic structure in the  
41 entire Pacific Ocean was  $\sim 15^\circ$  and that in the western Pacific Ocean was  $\sim 8^\circ$ . The lateral  
42 resolution of the radially anisotropic structure was worse because of the worse recovery  
43 of the checkerboard pattern in the Love wave test. The resolution was  $\sim 18^\circ$  in the entire  
44 Pacific Ocean and  $\sim 10^\circ$  in the western Pacific Ocean. The different spatial resolution in  
45 the Love and Rayleigh waves may affect the radially anisotropic structure. When we  
46 simply made radial anisotropy maps, there were many small-scale anomalies below the  
47 spatial resolution, which were randomly distributed in the entire Pacific Ocean. To  
48 diminish these small-scale anomalies, we applied a spatial low-pass filter at  $15^\circ$  for the

49 isotropic structure and  $18^\circ$  for the radially anisotropic structure to the results discussed in  
50 the context of the entire Pacific region and at  $8^\circ$  and  $10^\circ$  for the western Pacific region.

## 51 **S2 Jackknife error estimation**

52           Understanding the trade-off between the model resolution and error is helpful  
53 for interpreting inversion results. Panning and Romanowicz (2006) suggested that the  
54 bootstrap or jackknife error estimation was useful for the purpose and that estimated  
55 errors of both methods were virtually identical. Applying the bootstrap method to this  
56 study is not practical due to heavy computation, and thus we apply the jackknife error  
57 estimation.

58           We divide the original data into 10 subsets by random selection without  
59 duplication and then construct 10 jackknife data samples by removing one of the subsets  
60 from the original data. We calculate a phase-speed map for each of those jackknife  
61 samples. The average and standard errors are estimated following Panning and  
62 Romanowicz (2006) (Figure S12). The estimated errors are less than 0.02 km/s for the  
63 fundamental mode surface wave, and 0.05 km/s for higher modes. Large errors can be  
64 seen along the Pacific rim for higher modes, whereas errors are small in most of the

65 Pacific Ocean. The estimated errors of the phase speed maps are small enough to be used  
66 to construct local shear wave speed models.

67

68 Panning, M., Romanowicz, B., 2006. A three-dimensional radially anisotropic model of  
69 shear velocity in the whole mantle. *Geophys. J. Int.* 167, 361–379. doi:10.1111/j.1365-  
70 246X.2006.03100.x

71

## 72 **Supplemental Figure Captions**

73 Figure S1

74 Plot of the ray distribution of fundamental-mode (a) Rayleigh and (b) Love waves at a  
75 period of 83 s. Red lines indicate rays observed by BBOBSs. Blue triangles indicate  
76 BBOBS locations. Finite-width ray densities of the (c) Rayleigh and (d) Love waves. We  
77 counted the cells that were covered by the influence zone.

78 Figure S2

79 Result of the checkerboard resolution tests for fundamental-mode surface waves at a  
80 period of 83 s using  $10^\circ$  cells to assess the effects of different weighting schemes on the

81 data. (a) Result of the checkerboard resolution test for Rayleigh waves with no weighting  
82 scheme. (b) Result of the checkerboard resolution test for Rayleigh waves assigned a  
83 weight of 2.0. (c) Result of the checkerboard resolution test for Rayleigh waves assigned  
84 a weight of 3.0. (d–f) Same as for (a–c) but with Love waves. Recovered amplitudes in  
85 the eastern half of the Pacific Ocean were improved relative to the no-weighting scheme.

86

87 Figure S3

88 Results of the checkerboard resolution tests for fundamental-mode surface waves at a  
89 period of 83 s with (a, e) 6°, (b, f) 8°, (c, g) 12°, and (d, h) 16° cells for (a–d) Love and  
90 (e–h) Rayleigh waves.

91

92 Figure S4

93 (a) Age-bin-averaged  $\beta_{\text{iso}}$  and (b) age-bin-averaged radial anisotropy profiles of the  
94 Pacific Plate regions from the PAC-c model. In (a), the thin black contour lines show  
95 shear-wave speeds at 0.05 km/s intervals, whereas the thick black line shows the 1100 °C  
96 isotherms of the HSC model used in the modeling.

97

98 Figure S5

99  $\beta_{iso}$  as a function of the geotherm based on the HSC model at 5-Myr intervals from the

100 PAC-c model. Solid circles show the data at ages between 35 and 80 Ma, from which we

101 estimated the thermal coefficient of  $\beta_{iso}$ . Solid lines show the predicted shear-wave speed

102 profiles calculated with the equations shown in the figure. Different colors correspond to

103 different depths.

104 Figure S6

105 Isotropic shear-wave speed maps of the PA-c model (a–c), PA-age model (d–f), and

106 their difference (g–i) at depths of 50, 75, and 100 km, respectively.

107 Figure S7

108 Comparison between the PAC-age model and the previous models of  $\delta\beta_{iso}$  (%) at depths

109 of 50, 100, and 200 km.

110 Figure S8

111 Same as for Figure S7 but with radial anisotropy.

112 Figure S9

113 Results of the synthetic tests for estimating the depths of the negative peaks of the vertical  
114 gradient of  $\beta_{\text{iso}}$ . Red, blue, and black lines show the speed profiles of the  $\beta_{\text{SV}}$ ,  $\beta_{\text{SH}}$ , and  
115  $\beta_{\text{iso}}$ , respectively. Broken lines show the input models, whereas solid lines show the  
116 recovered models. The discontinuity depths of the input models are indicated by black  
117 arrows at (a) 50, (b) 60, (c) 90, (d) 120, and (e) 140 km, respectively. (f) Comparisons  
118 between the recovered negative peak depths and the input discontinuity depths for  $\beta_{\text{SV}}$ ,  
119  $\beta_{\text{SH}}$ , and  $\beta_{\text{iso}}$ .

120 Figure S10

121 Comparison between (a–c) PAC-age, (d–f) PAC-age-exOBS, and (g–i) their difference at  
122 depths of 50, 100, and 200 km, respectively.

123 Figure S11

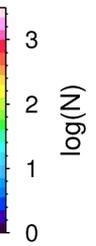
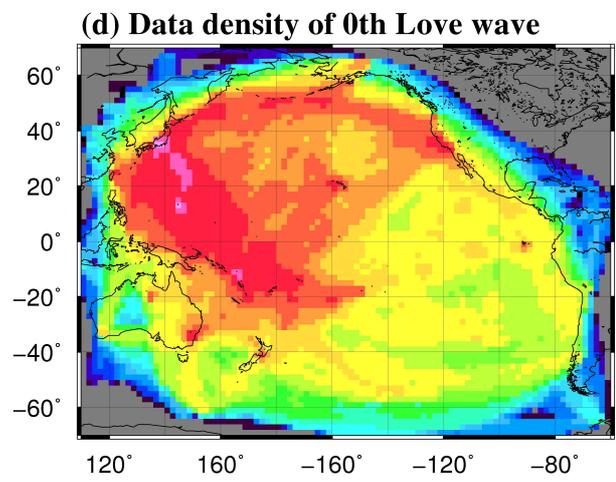
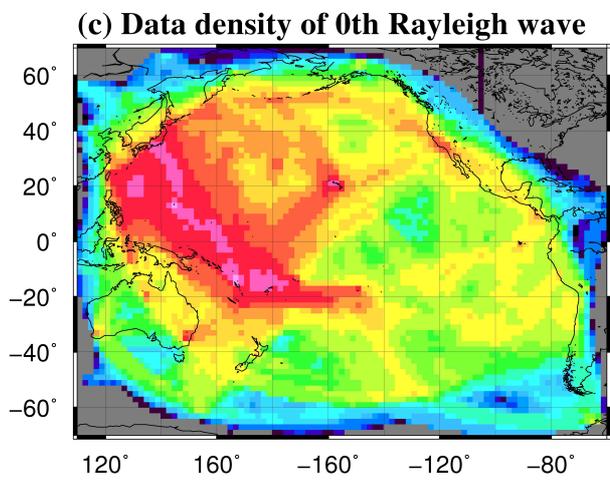
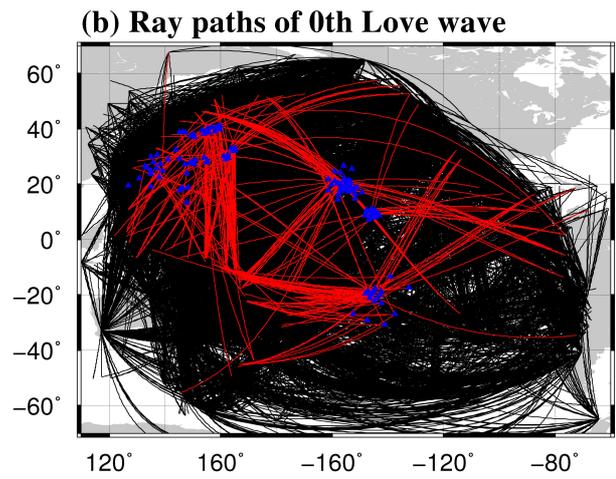
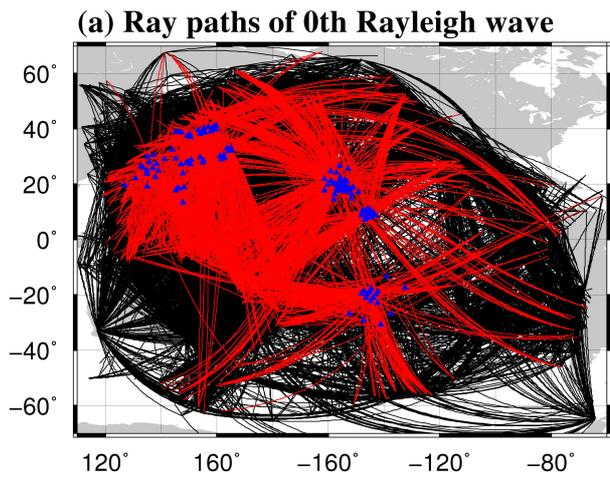
124 Same as for Figure 10 but using the plate model of Parsons and Sclater (1977) to  
125 estimate the mantle temperature.

126 Figure S12

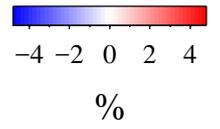
127 Standard errors of phase speeds calculated by using a jackknife approach for the  
128 fundamental mode surface wave at periods of 50 and 100s (left and middle), and the first

129 higher mode at a period of 100 s (right). Upper panels show the results for Love wave

130 and lower panels for Rayleigh wave.



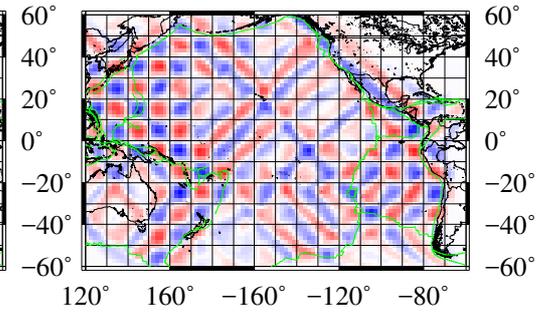
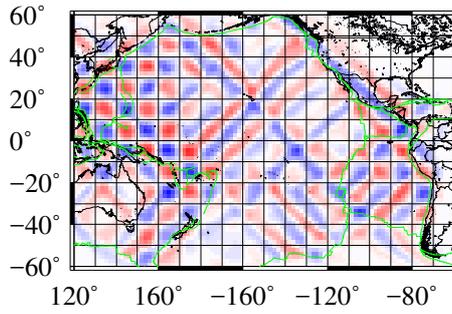
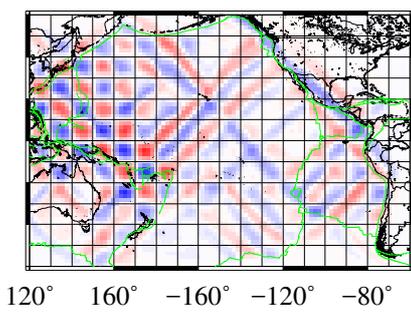
**Figure S1**



**(a) No Weight: Rayleigh**

**(b) Weight x2: Rayleigh**

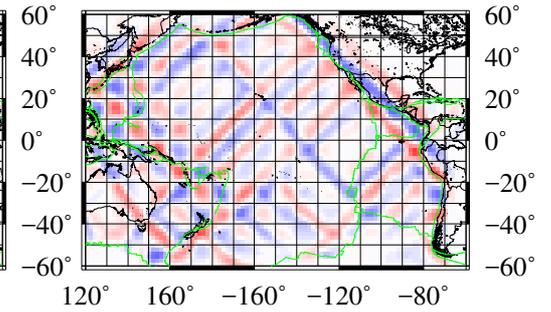
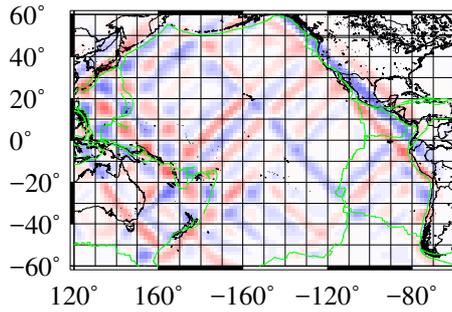
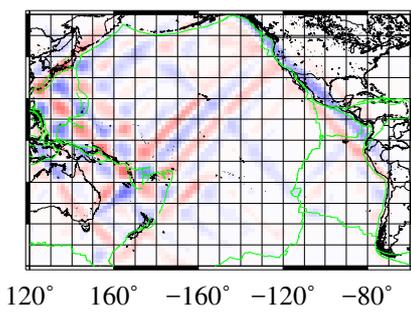
**(c) Weight x3: Rayleigh**



**(d) No Weight: Love**

**(e) Weight x2: Love**

**(f) Weight x3: Love**



**Figure S2**

# Love

# Rayleigh

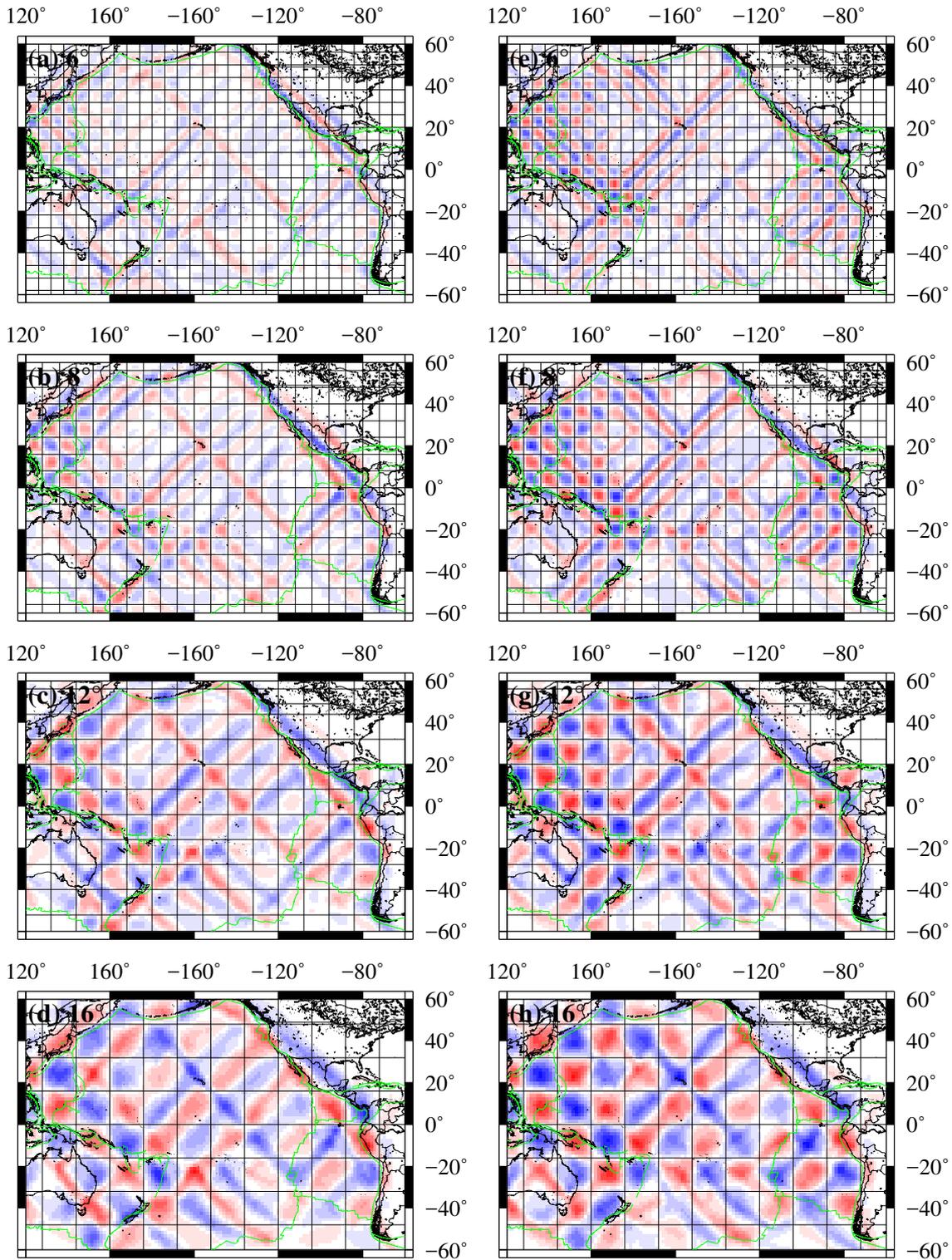
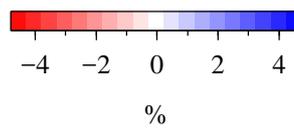
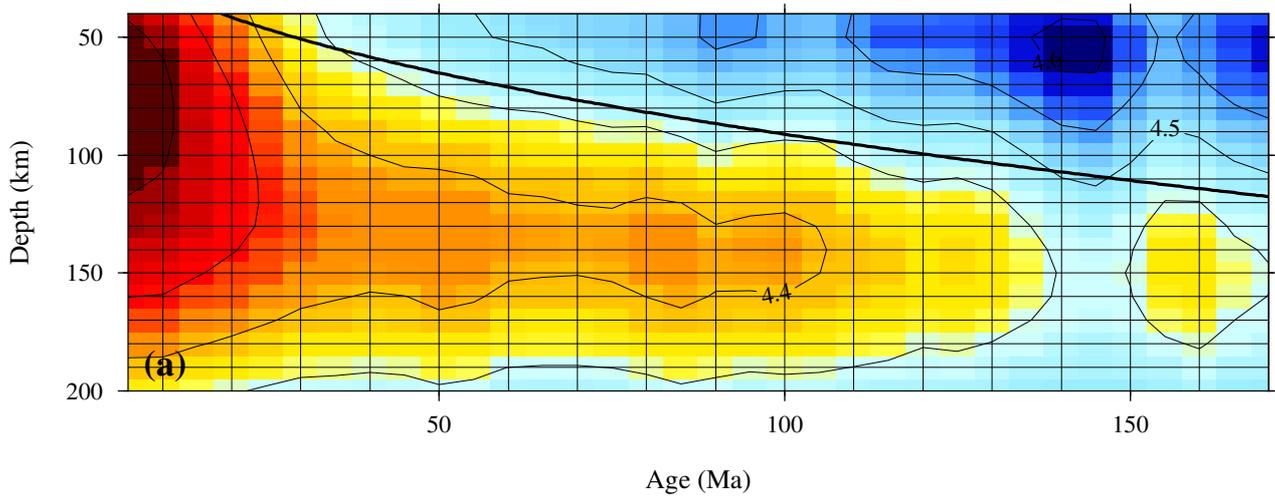


Figure S3



$\beta_{\text{iso}}$



$\xi$

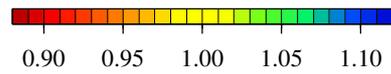
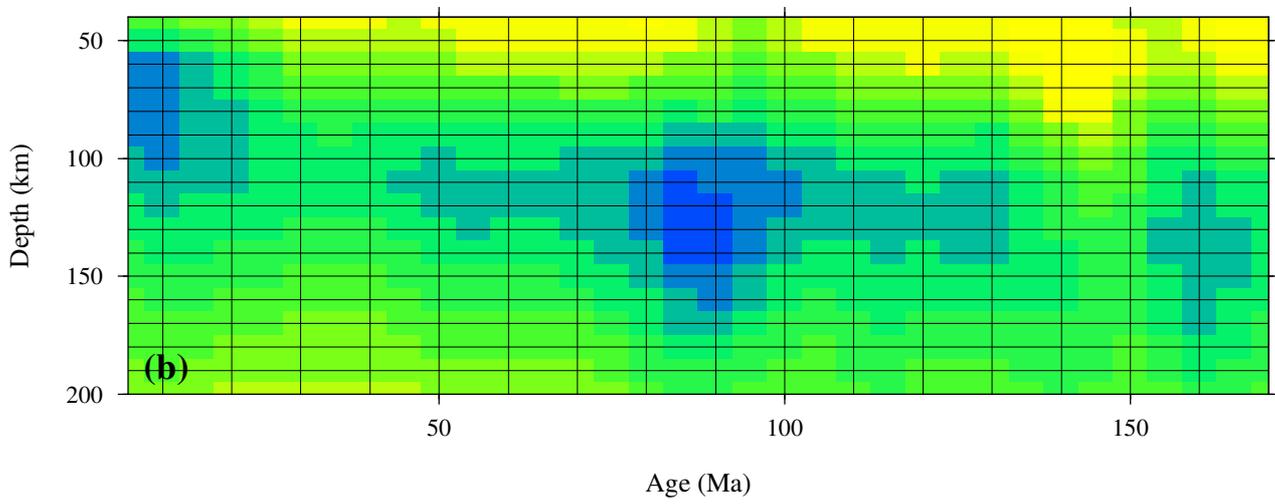


Figure S4

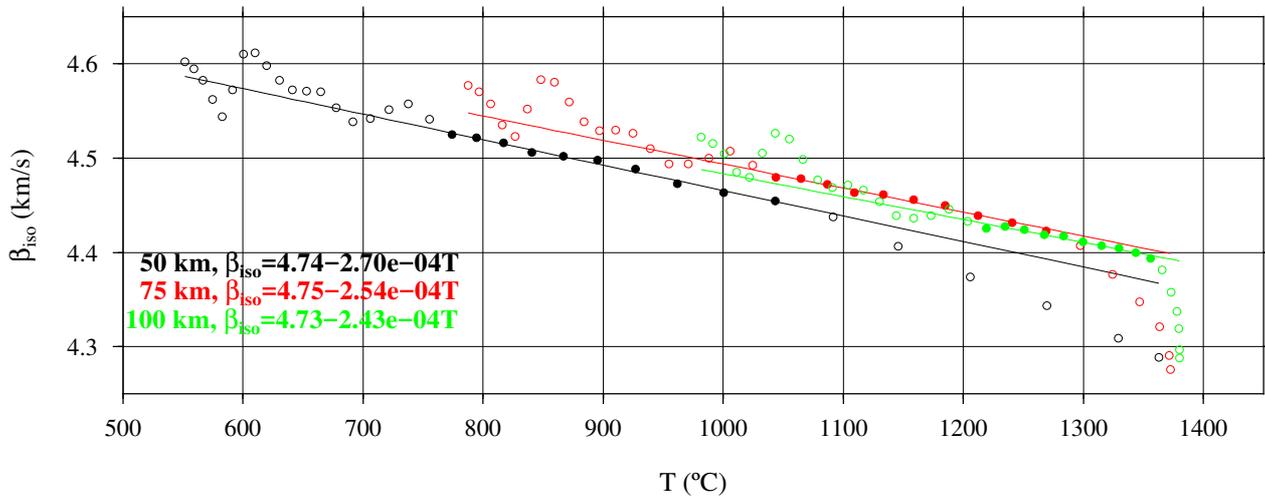


Figure S5

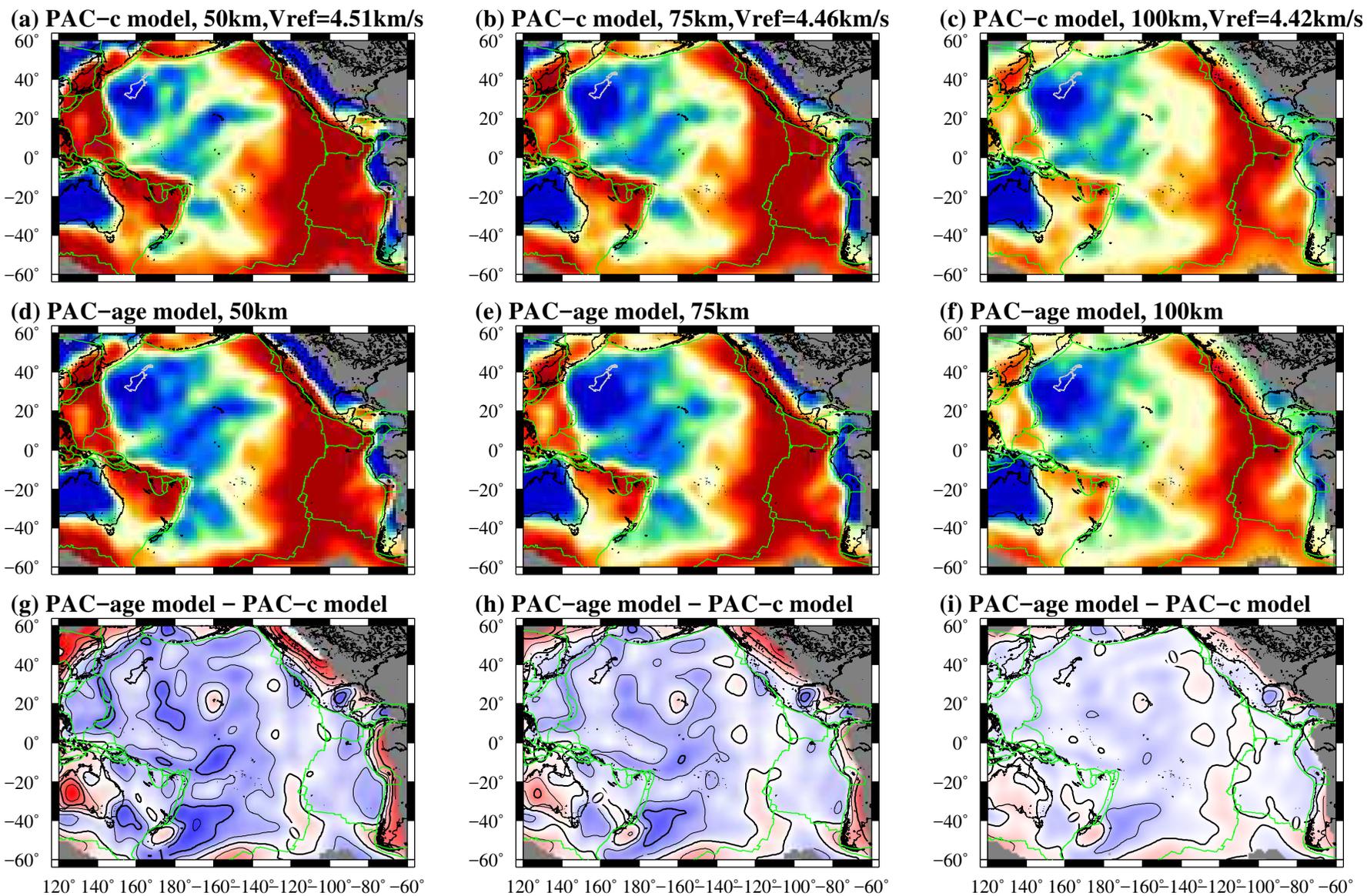
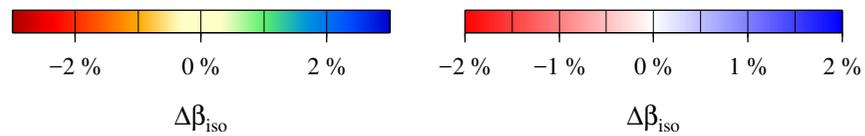
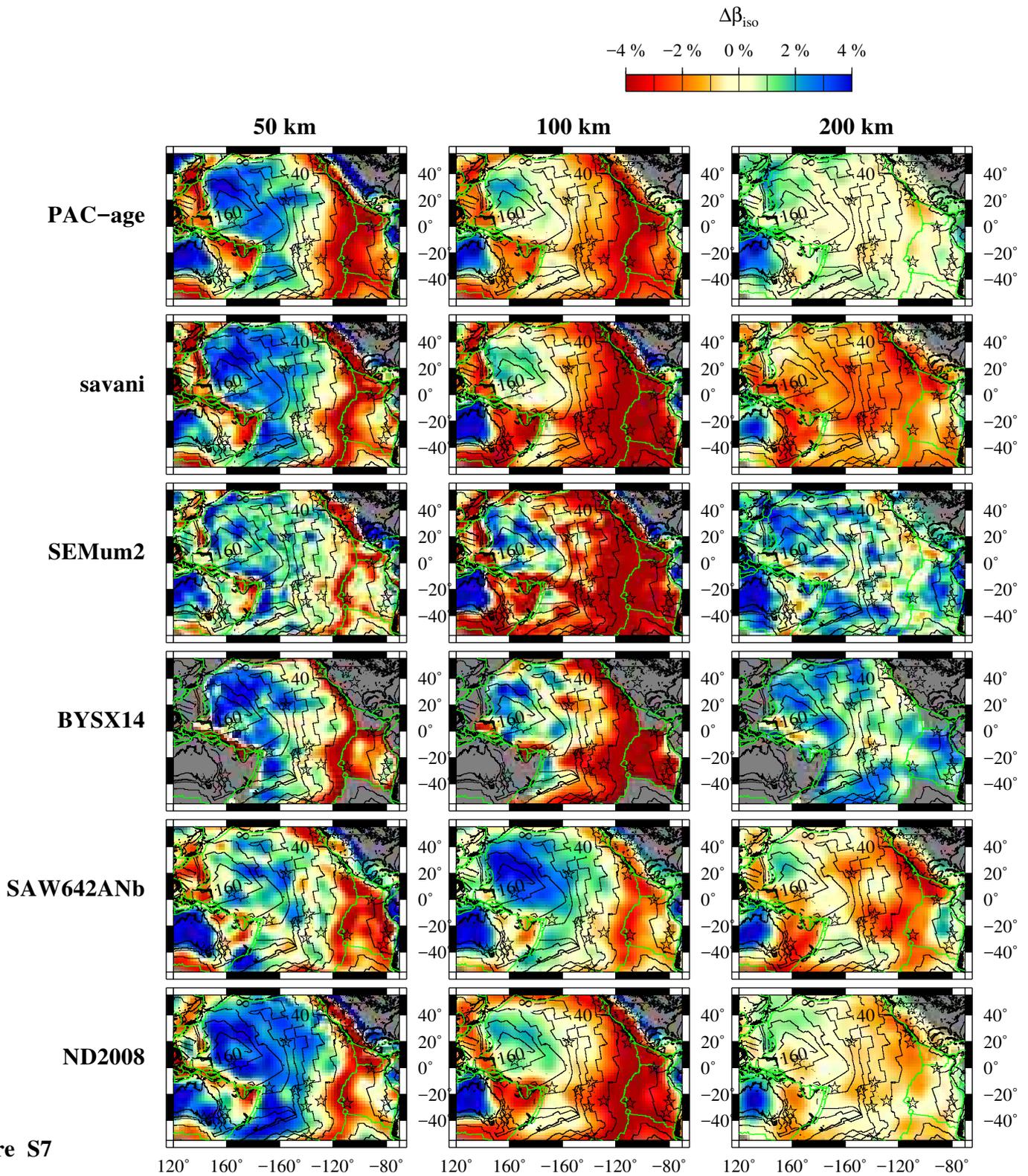
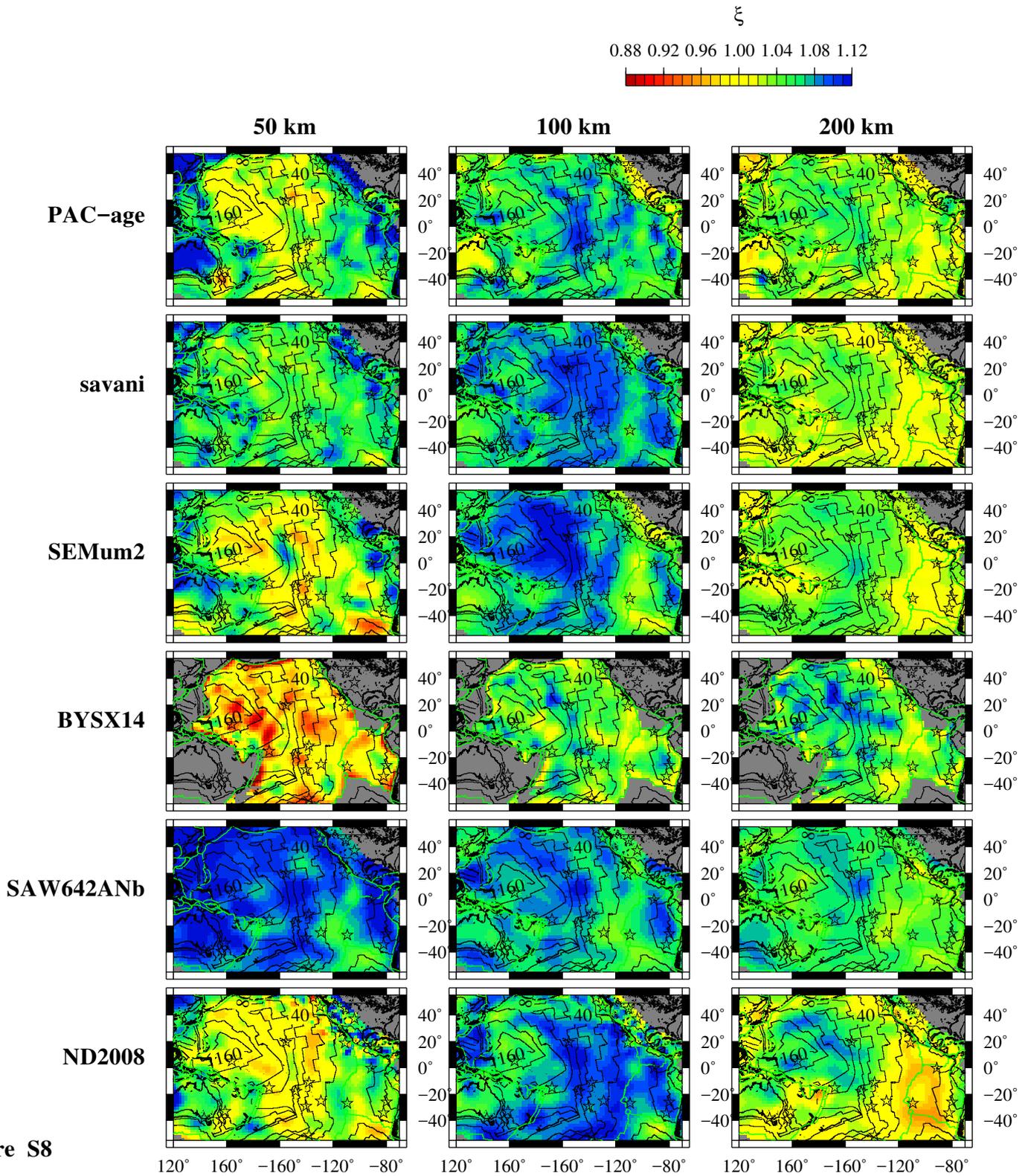


Figure S6

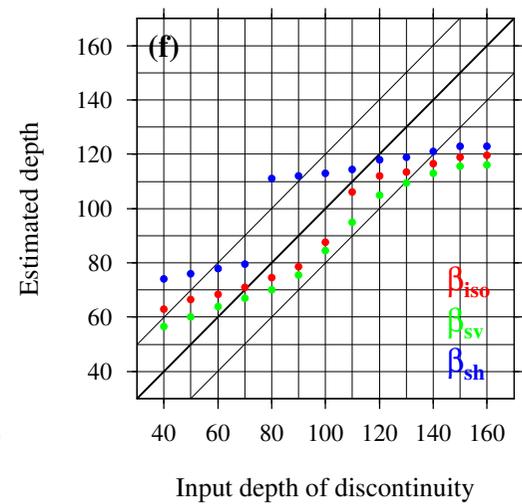
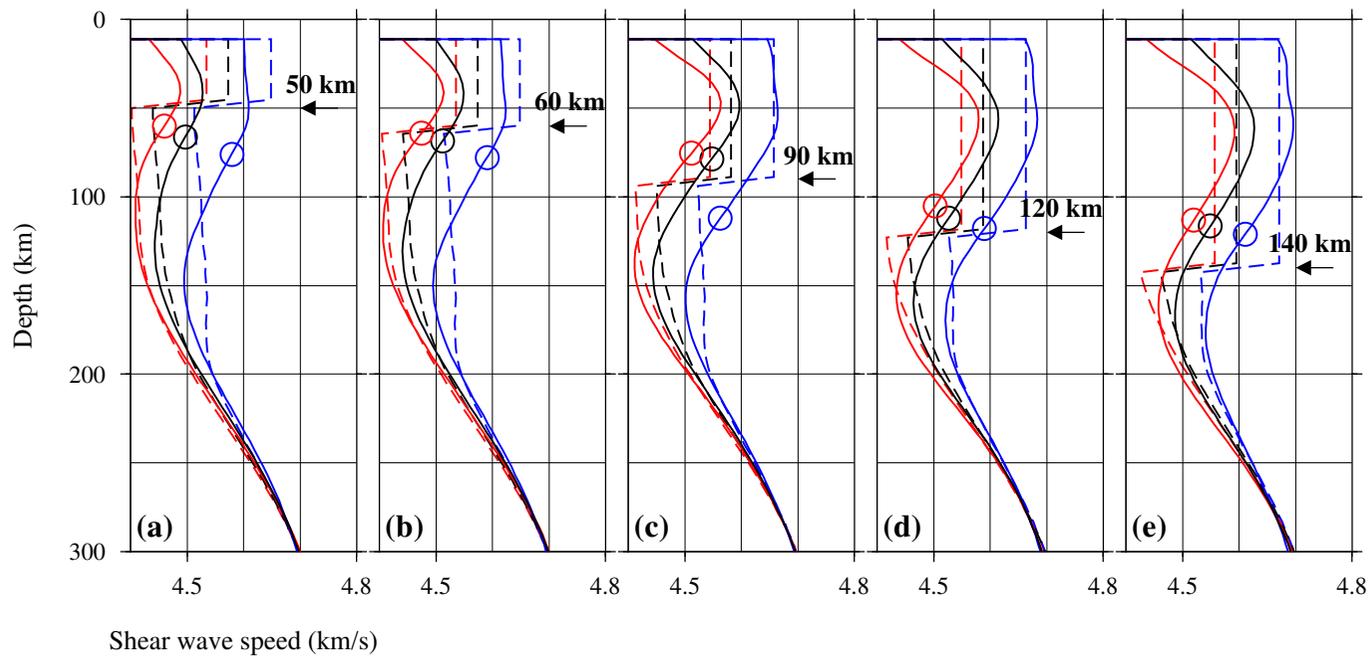




**Figure S7**

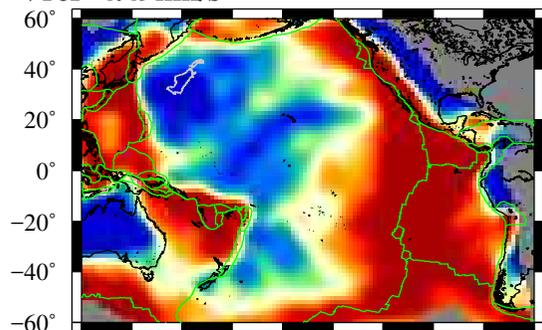


**Figure S8**

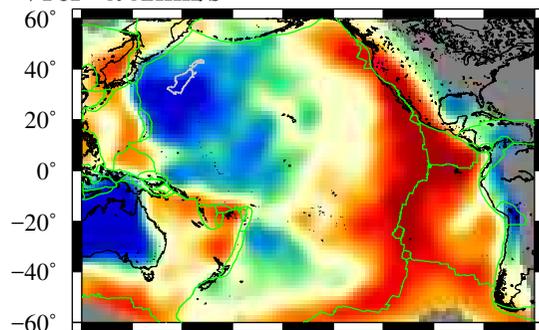


**Figure S9**

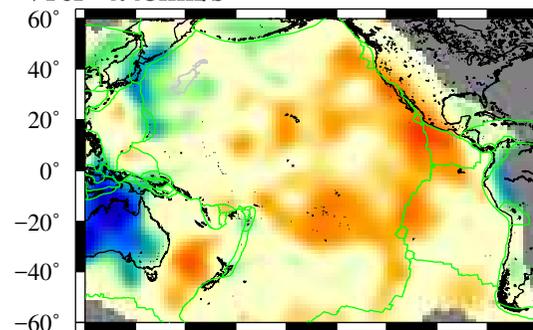
**(a) PAC-age model at 50km**  
 $V_{ref}=4.49\text{km/s}$



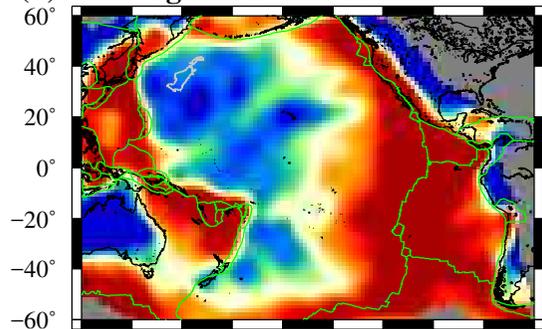
**(b) PAC-age model at 100km**  
 $V_{ref}=4.41\text{km/s}$



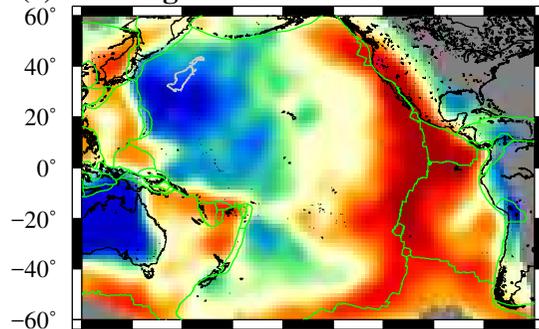
**(c) PAC-age model at 200km**  
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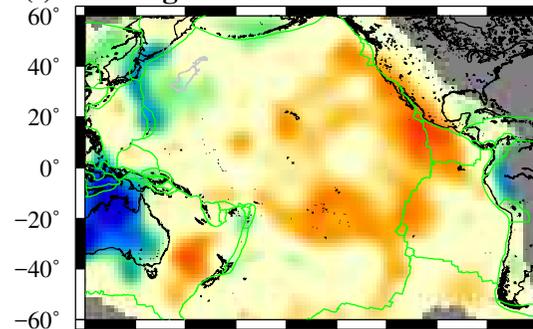
**(d) PAC-age-exOBS model**



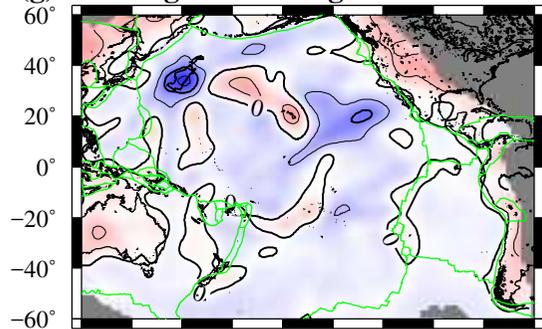
**(e) PAC-age-exOBS model**



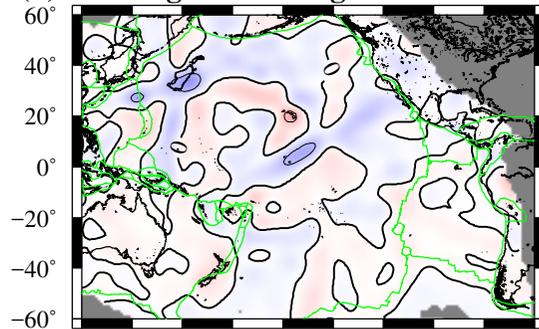
**(f) PAC-age-exOBS model**



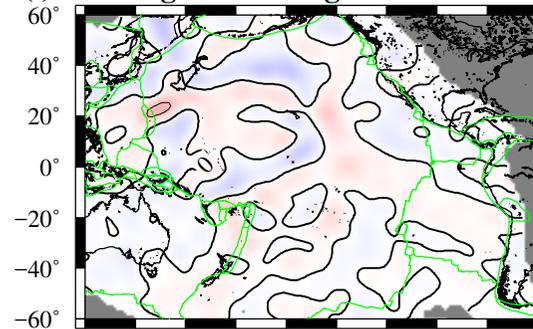
**(g) PAC-age - PAC-age-exOBS**



**(h) PAC-age - PAC-age-exOBS**



**(i) PAC-age - PAC-age-exOBS**

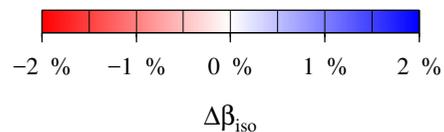
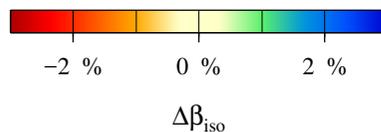


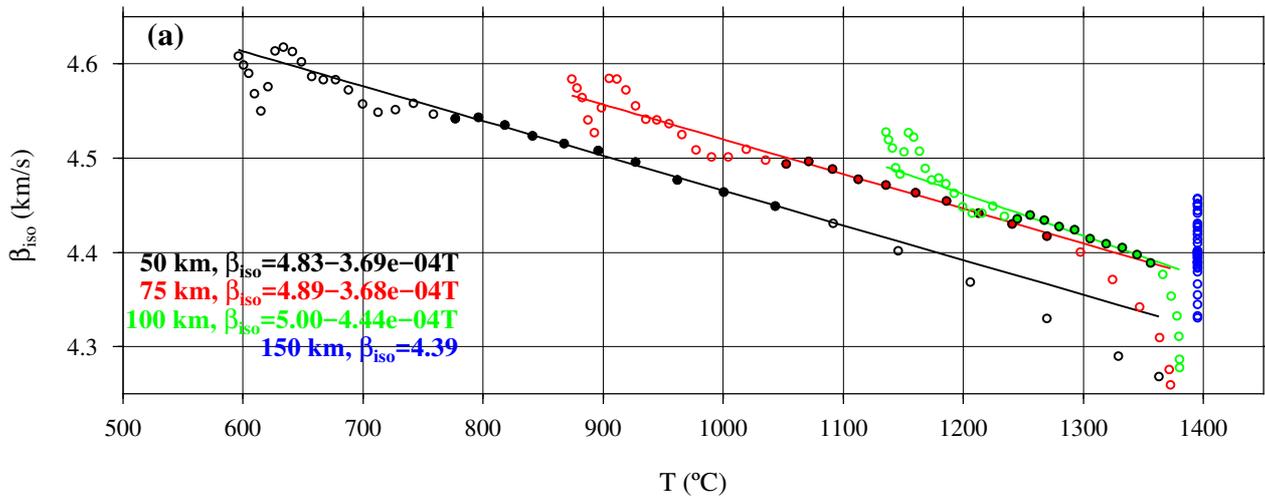
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120° 140° 160° 180° -160° -140° -120° -100° -80° -60°

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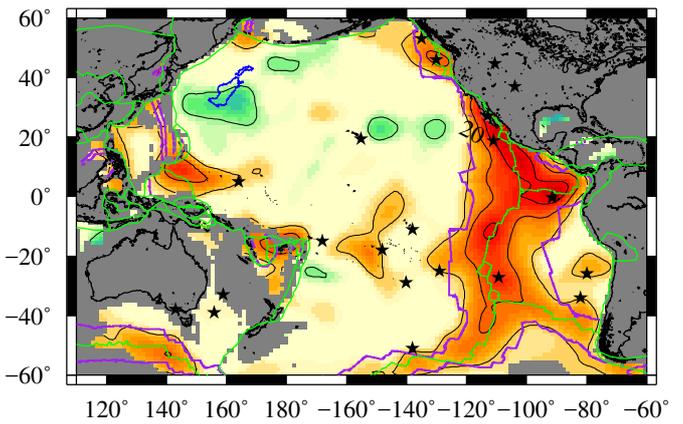
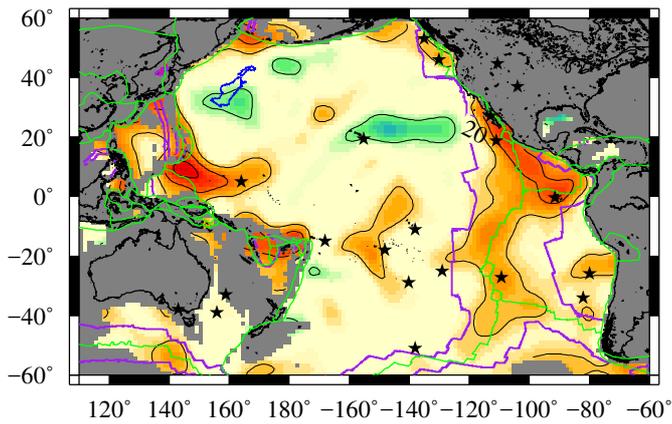
**Figure S10**





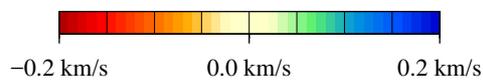
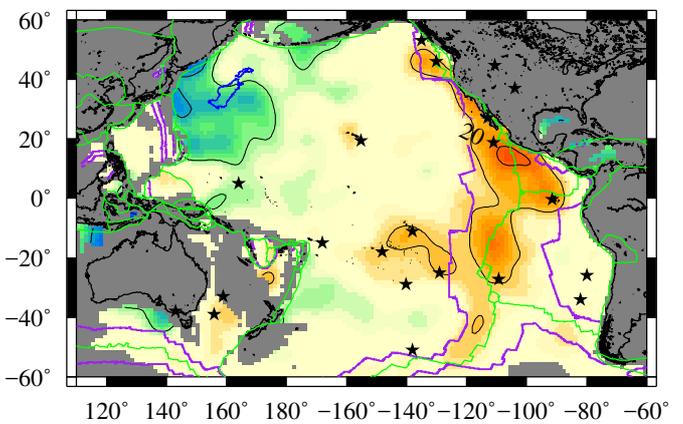
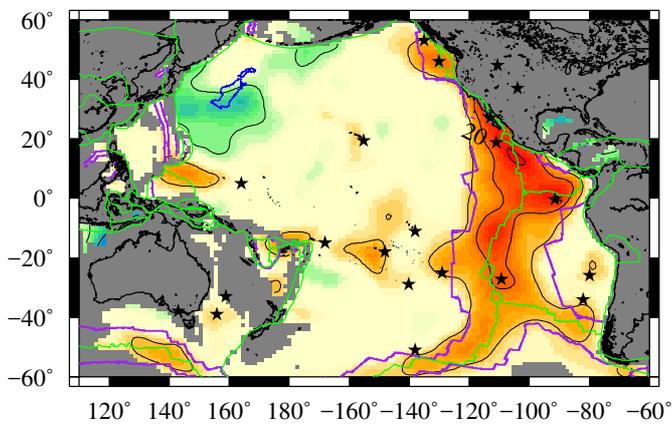
(b) 50 km

(c) 75 km



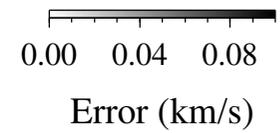
(d) 100 km

(e) 150 km

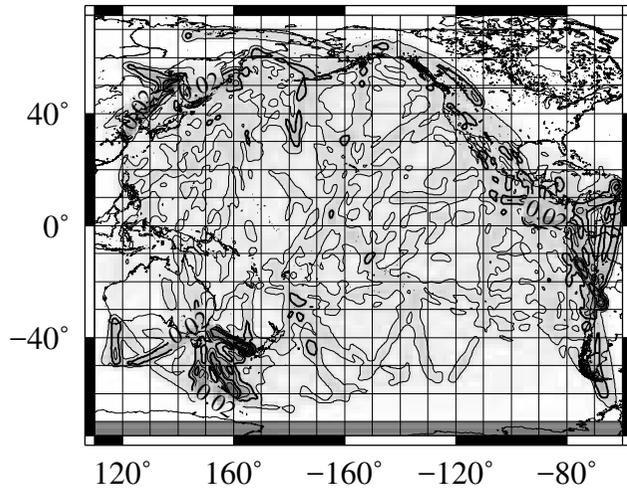


$\Delta\beta_{\text{iso}}$

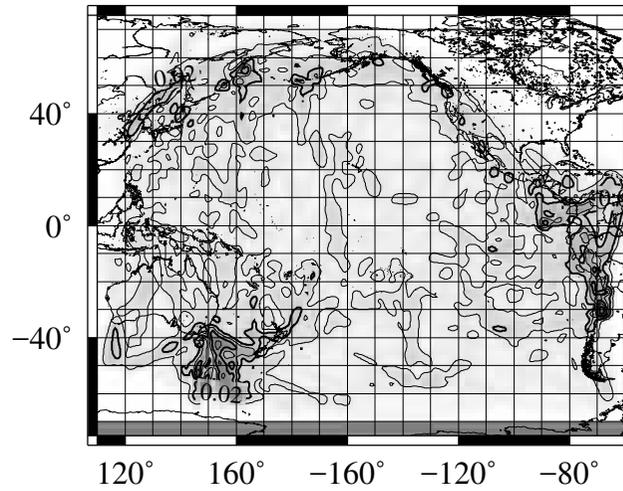
Figure S11



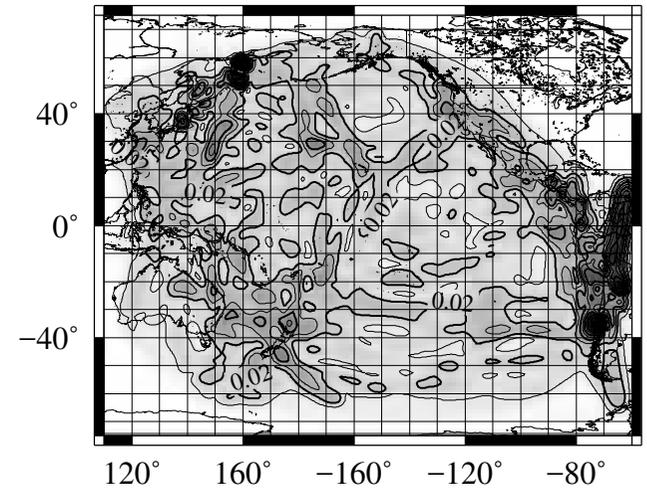
0th Love 50 s



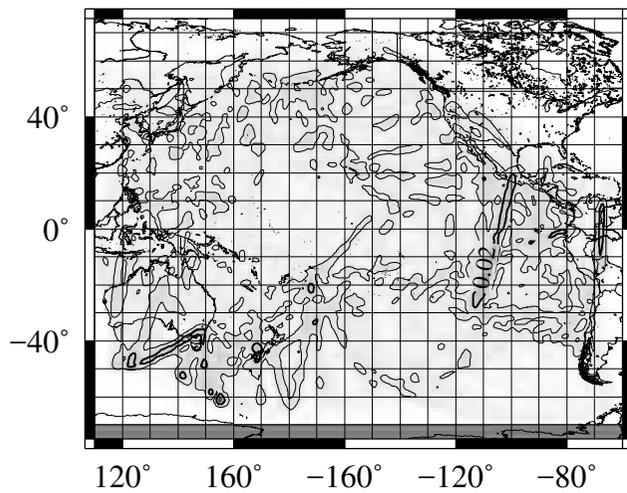
0th Love 100 s



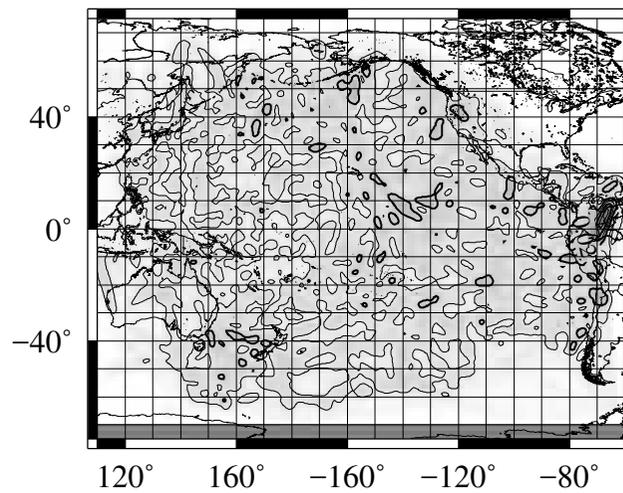
1st Love 100 s



0th Rayleigh at 50 s



0th Rayleigh at 100 s



1st Rayleigh 100 s

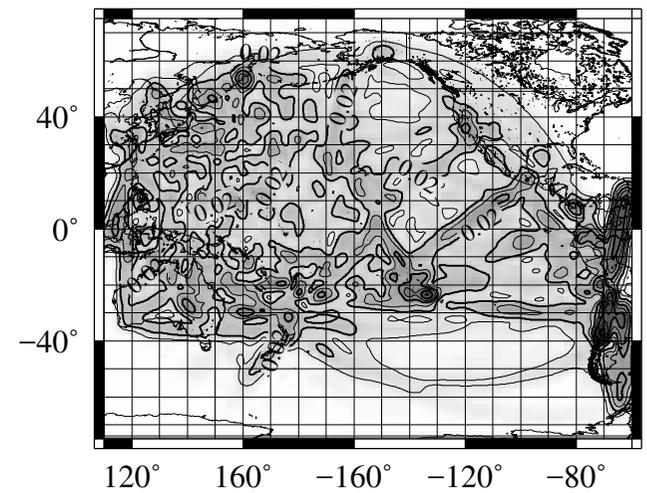


Figure S12