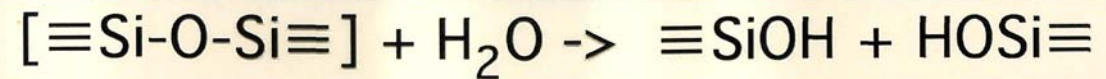
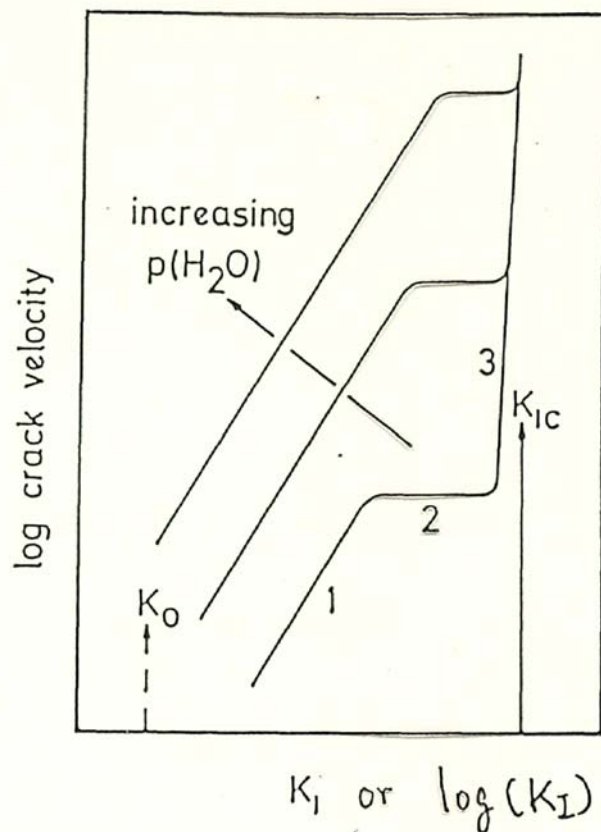


# Stress Corrosion Cracking (Sub-Critical Crack Growth) and its Implication for Slow Slip

Osam SANO

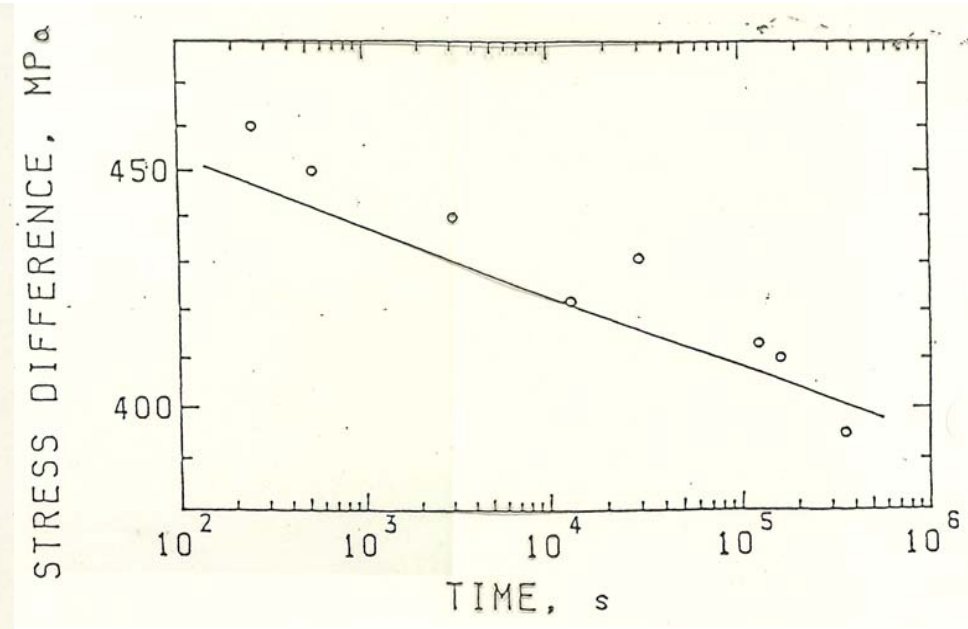
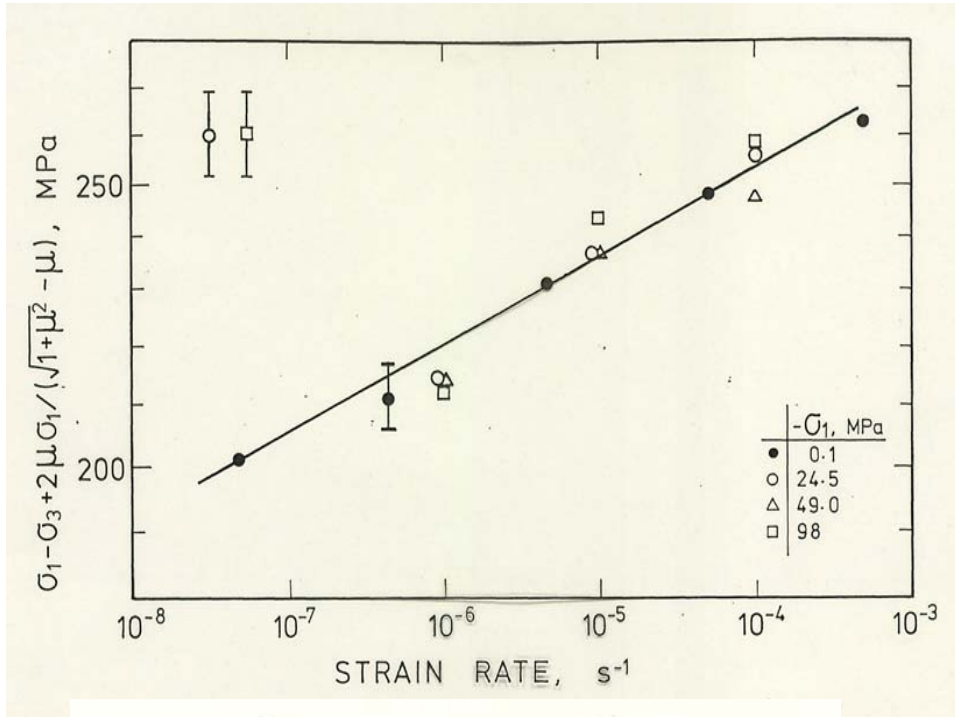
Cracks grow slowly even under critical state of stress, known as sub-critical crack growth.



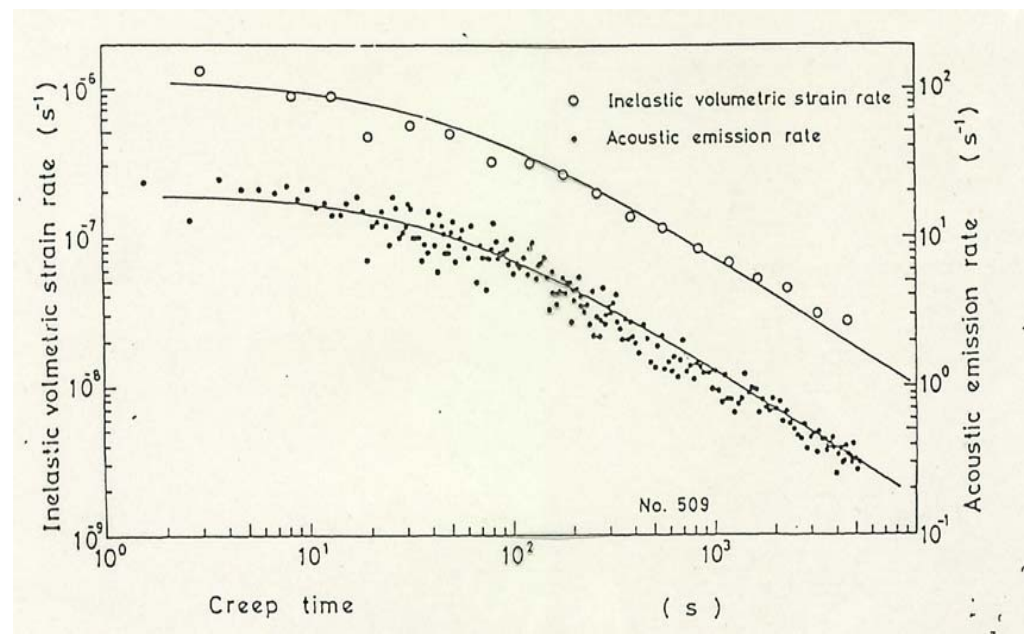
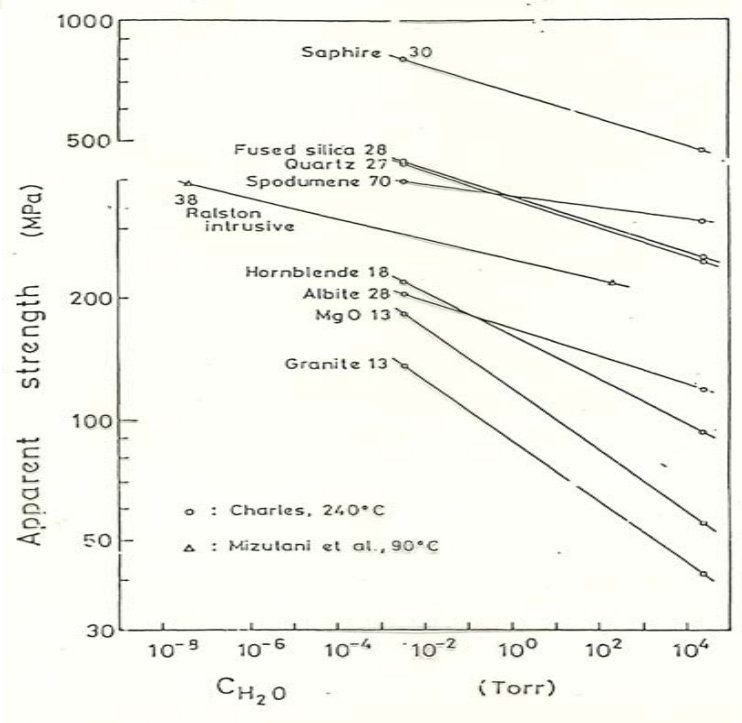
$$V \propto K_I^n \exp(-E/kT)$$

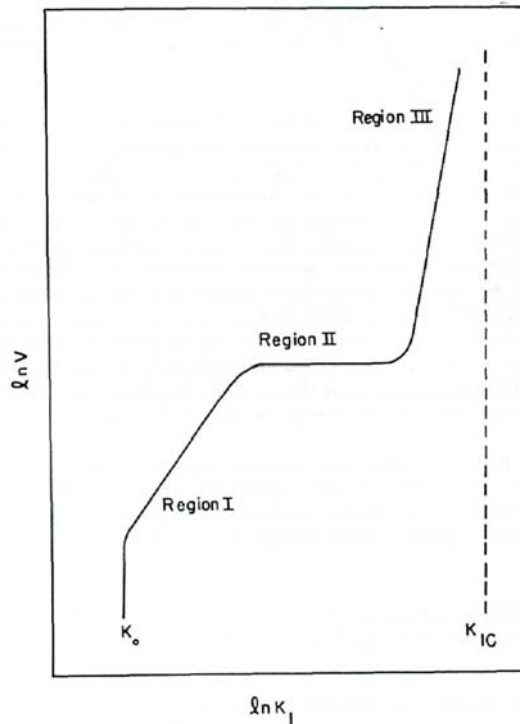
$$V \propto \exp[-(E - \alpha K_I)/kT]$$

PURPOSE:  $10^{-11}$  m/s or lower



↑ Data by Kranz (1980) were re-plotted.





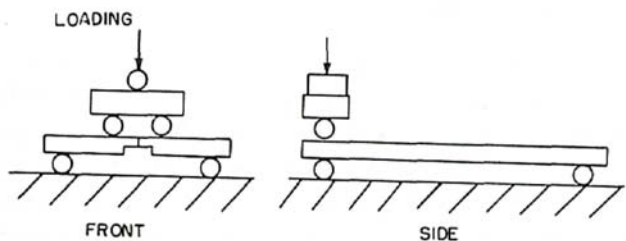
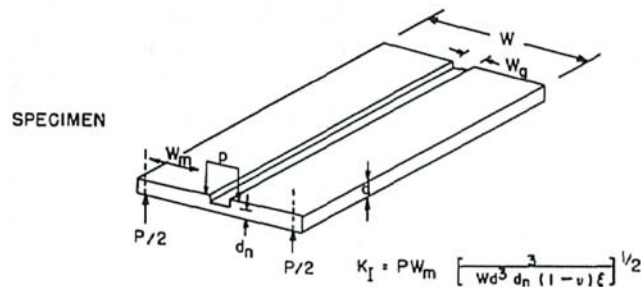
$$dC/dt = A_1 K_I^n$$

$$K_I = A_2 \sigma \sqrt{C}$$

$$dC/dt = A_1 A_2^n \sigma^n C^{n/2}$$

$$[C^{1-n/2} - C_0^{1-n/2}] / (1-n/2) = A_1 A_2^n \sigma^n t$$

$$C_0 / (dC_0/dt) = (n/2 - 1) t$$



Three years are required for extension of one meter under constant velocity of  $10^{-8}$  m/s. As  $K$  is proportional to the square of crack length,  $dc/dt$  will be accelerated.

**Scaling?**  $C_{\max}$  for 10 MPa is 0.02 m. Is it OK?

$C_{\max}$  for 100 hPa is 19 km...

$G_c = 60 \sim 100$  J/m<sup>2</sup> for observed  $K_c$ .

82 days for  $C_0=1$ m,  $dC_0/dt=1e^{-8}$  m/s, or 1 m and  $2 e^{-10}$  m/s for 3 years.

**Arrest mechanisms?**

$$y = \lambda P = (Bc+D)P$$

$$dy/dt = BP dc/dt + (Bc+D)dP/dt$$

(1) Constant Load

$$dc/dt = (dy/dt)/BP$$

(at constant  $dy/dt$ .)

(2) Constant  $dy/dt$

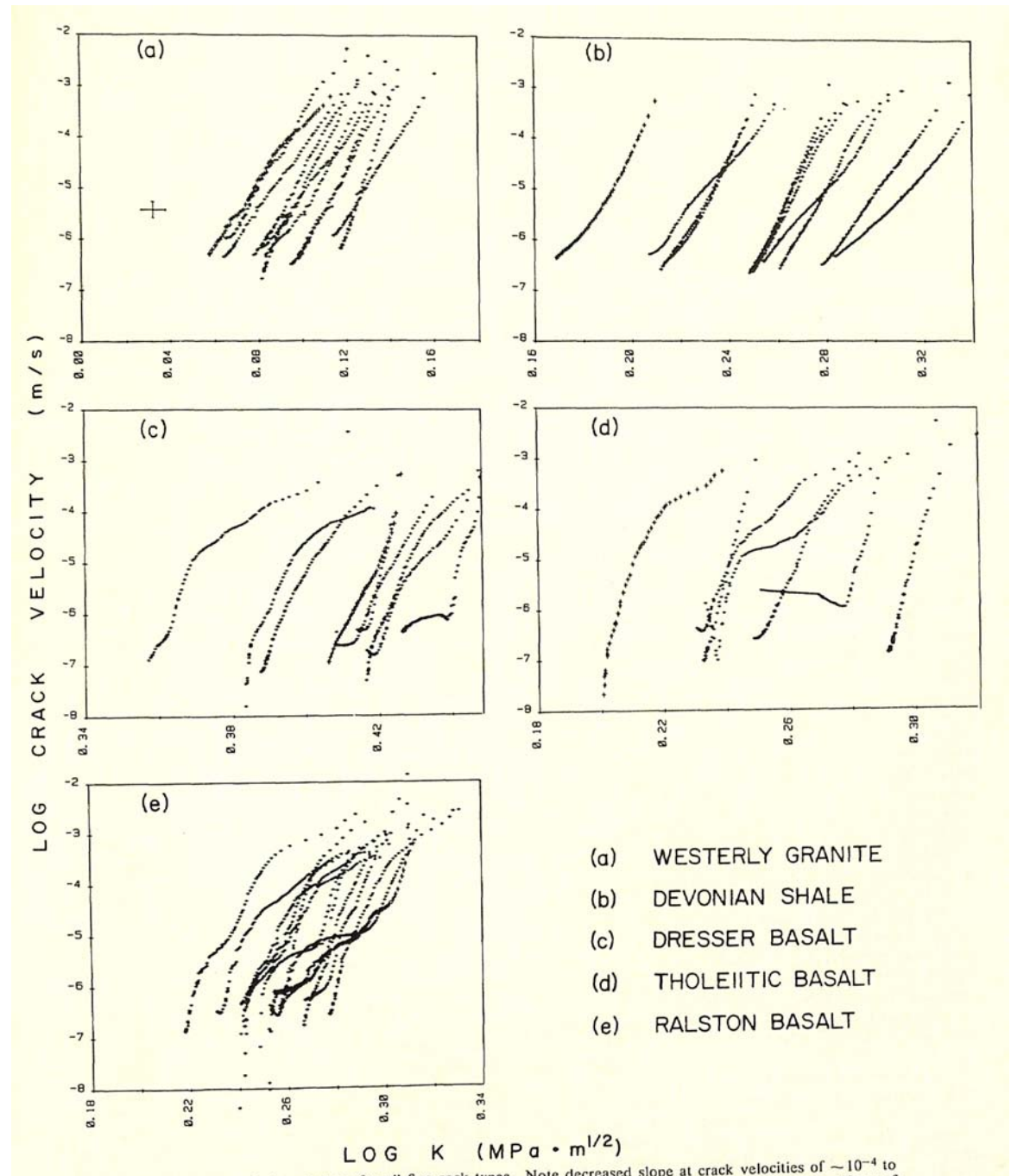
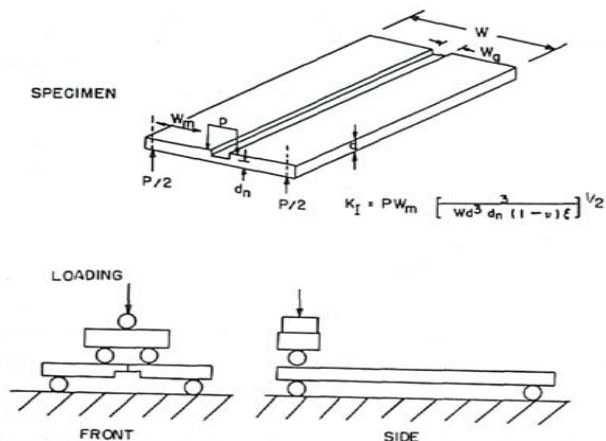
$$dc/dt = (dy/dt)/BP$$

(at constant  $P$ .)

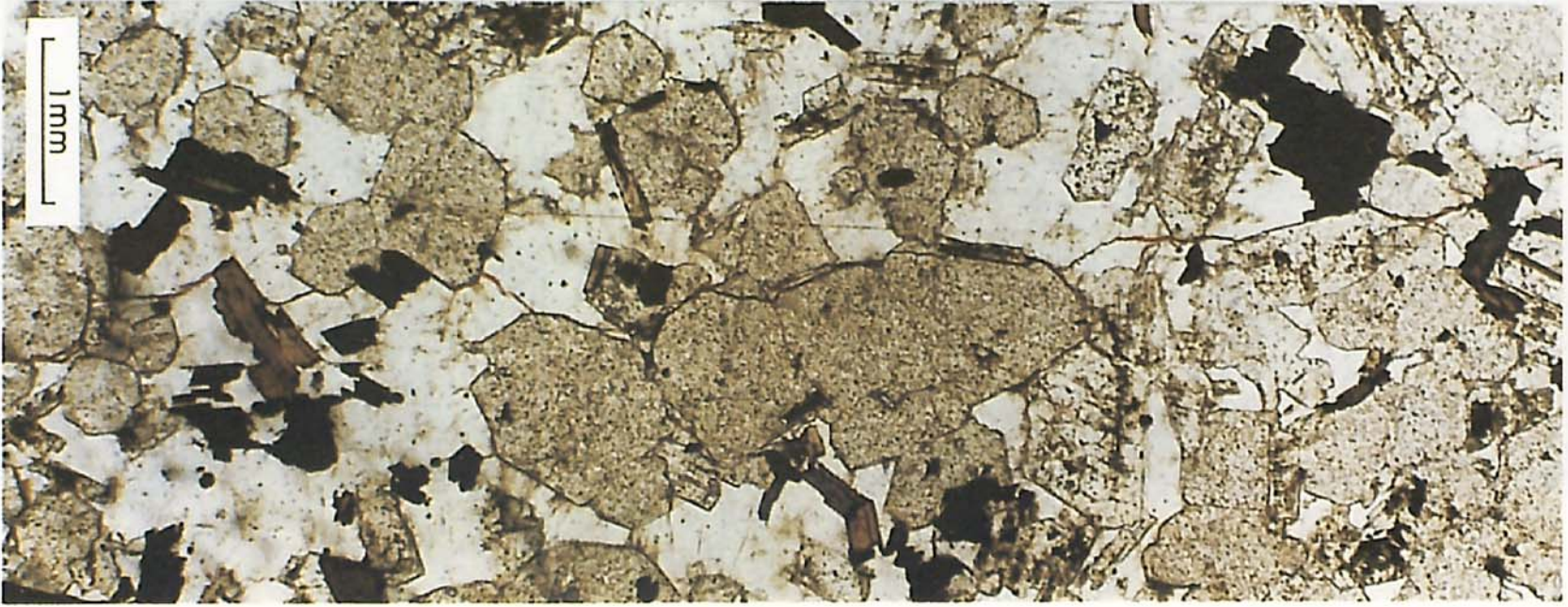
(3) Constant  $y$  (Relaxation)

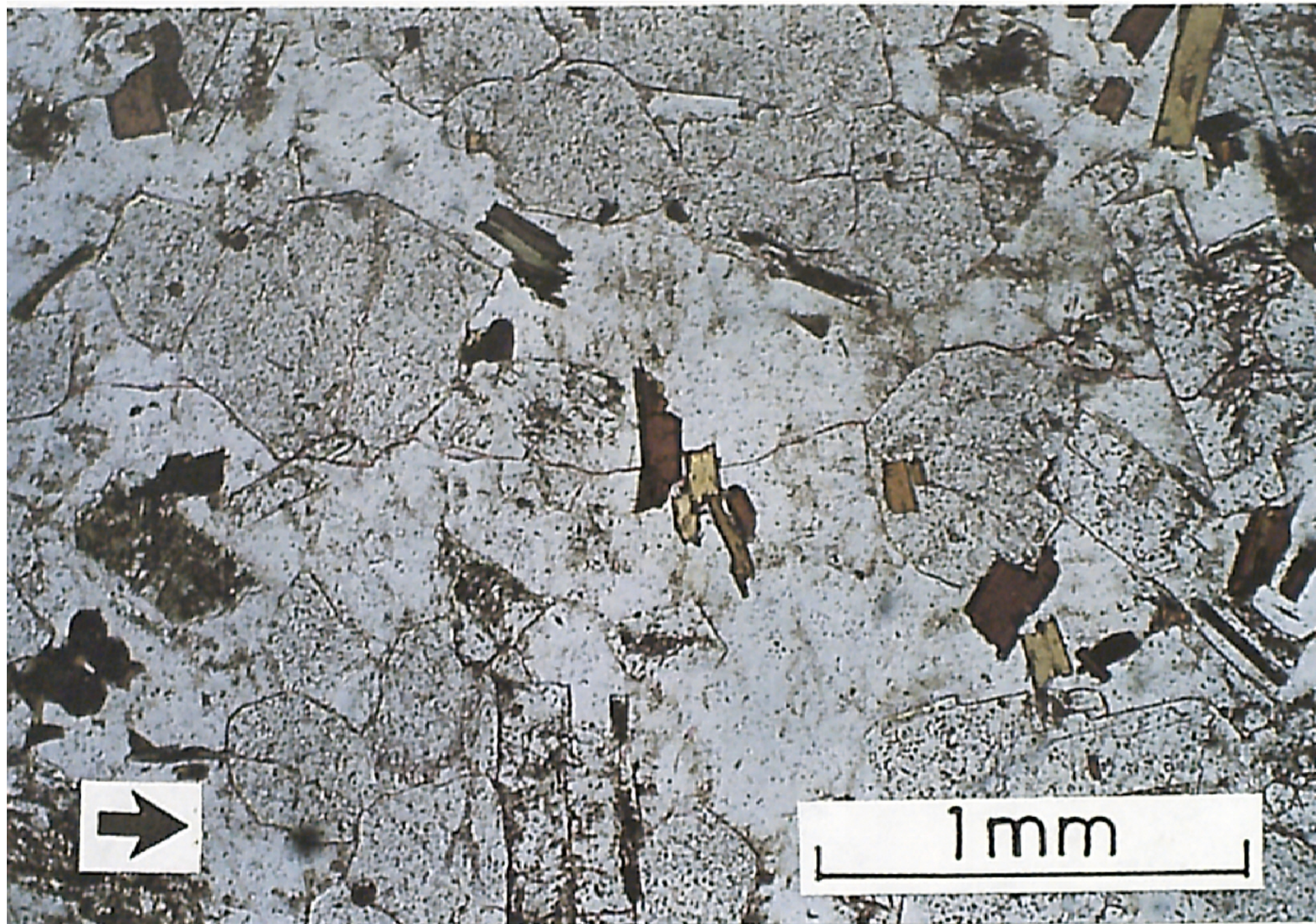
$$dc/dt = - (P_i \lambda_i / BP^2) dP/dt$$

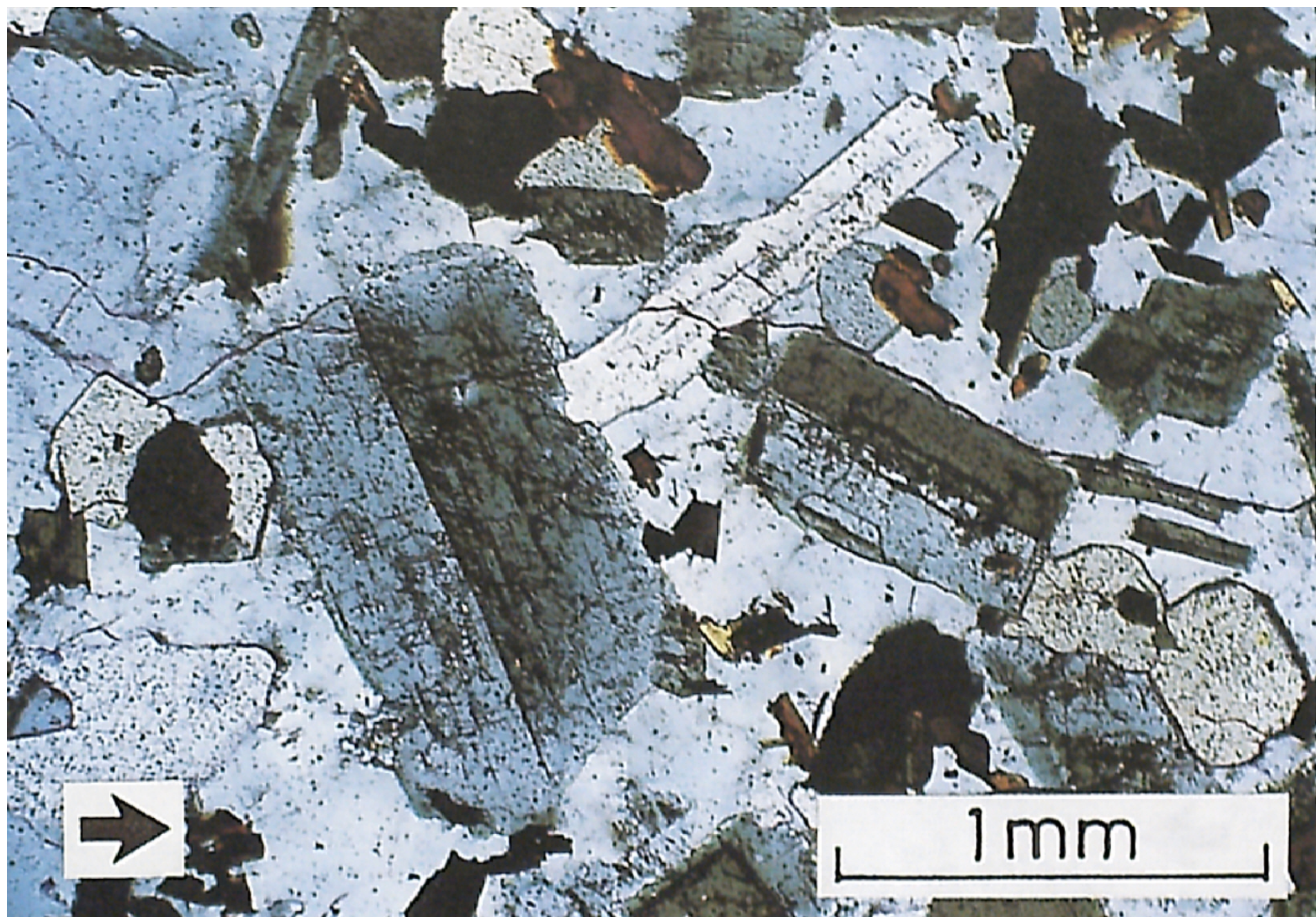
(Red letters indicate observation)

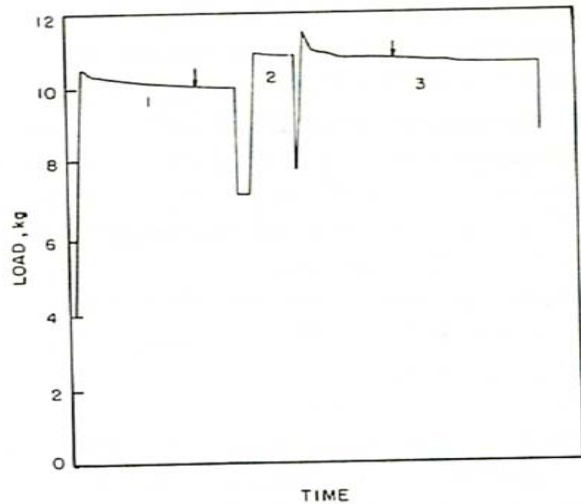
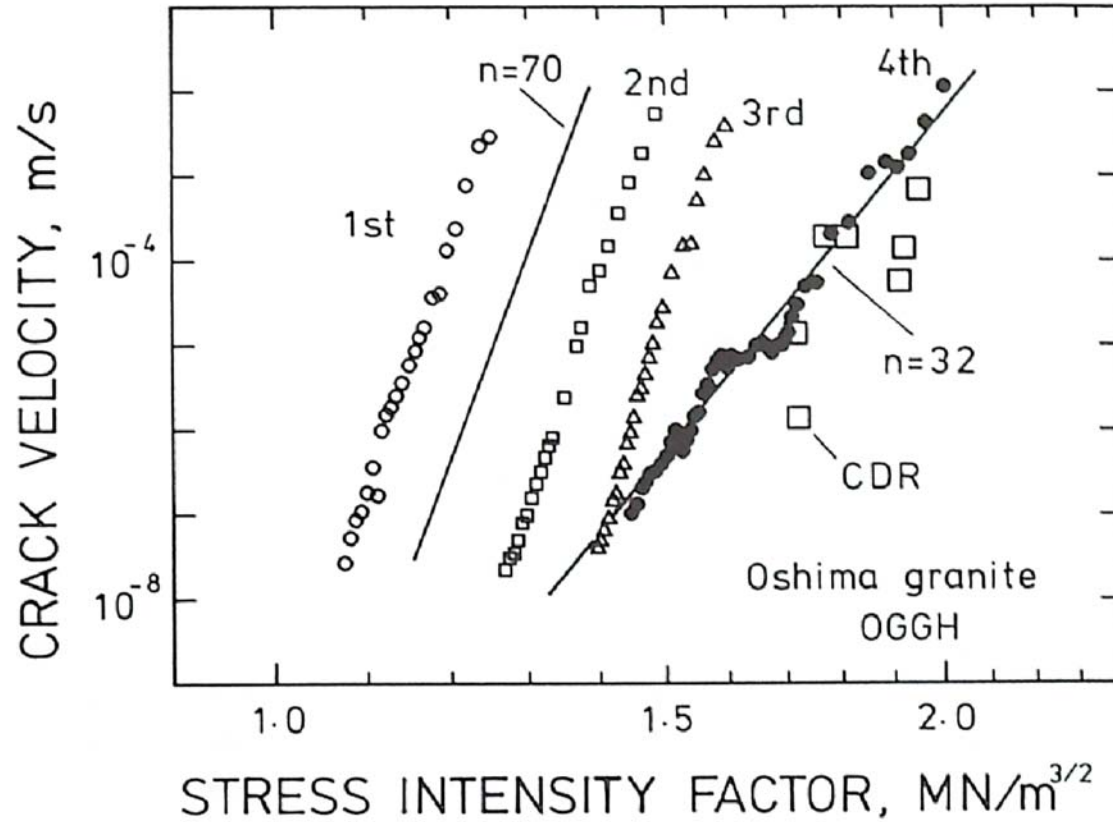
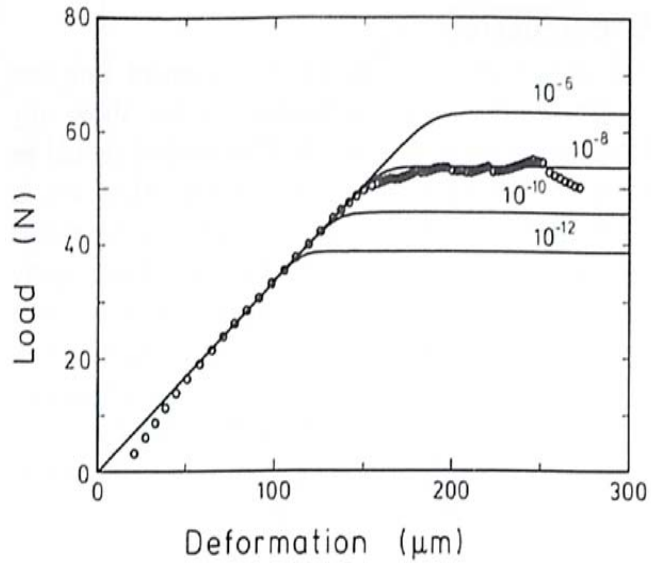


(After Swanson, J. G. R., 1984)





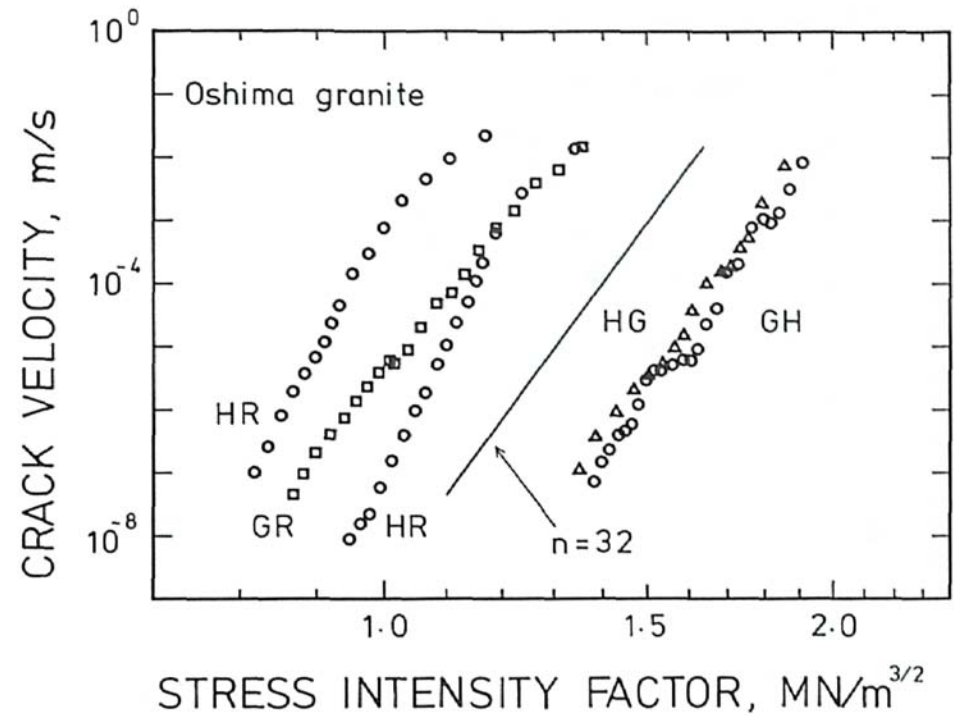
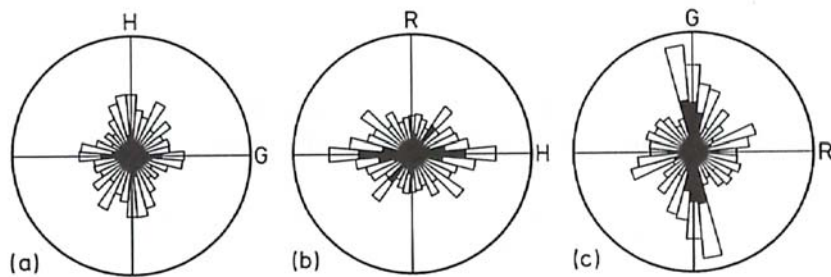
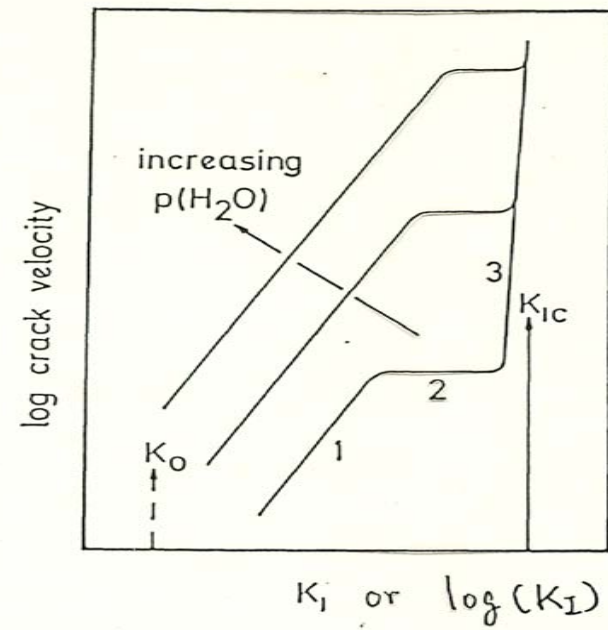
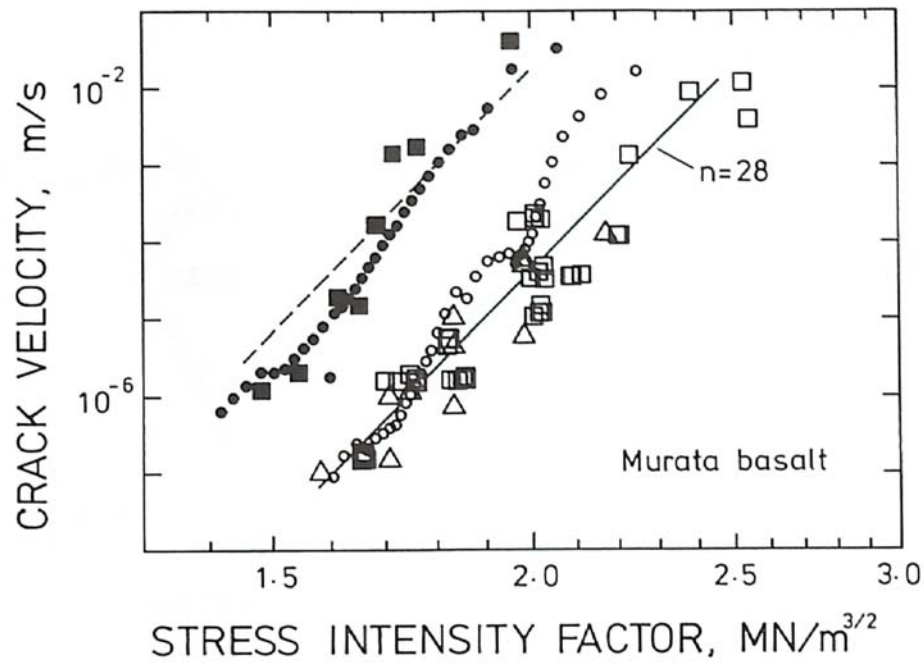


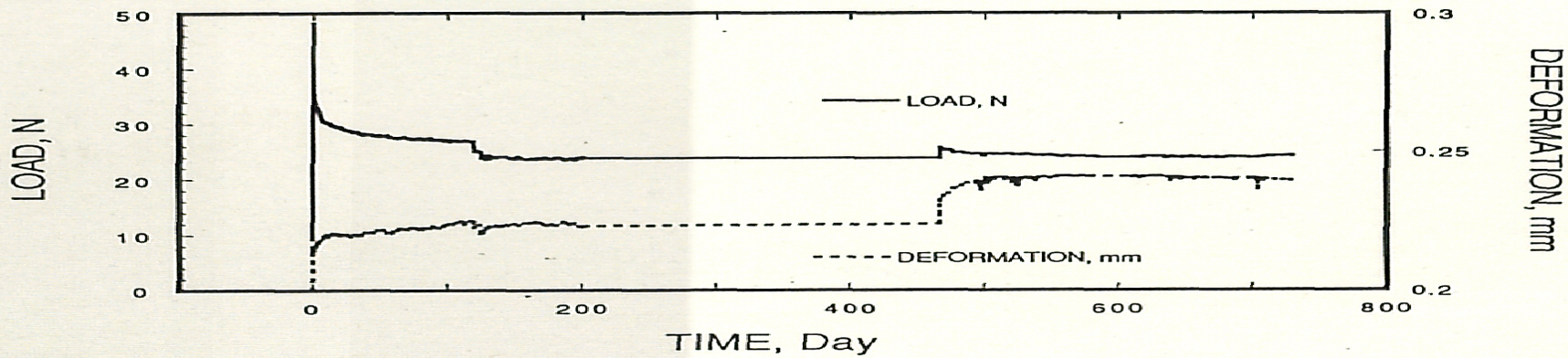
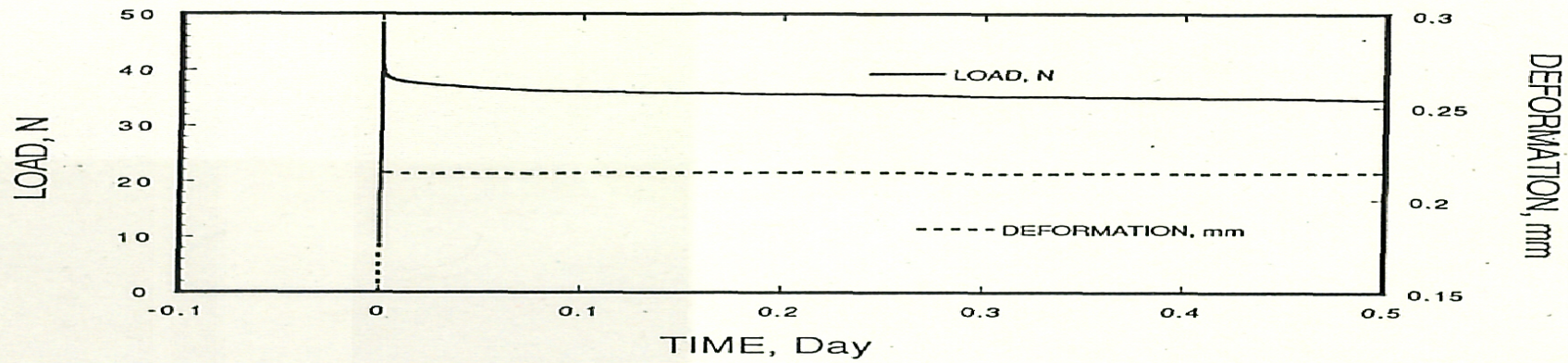
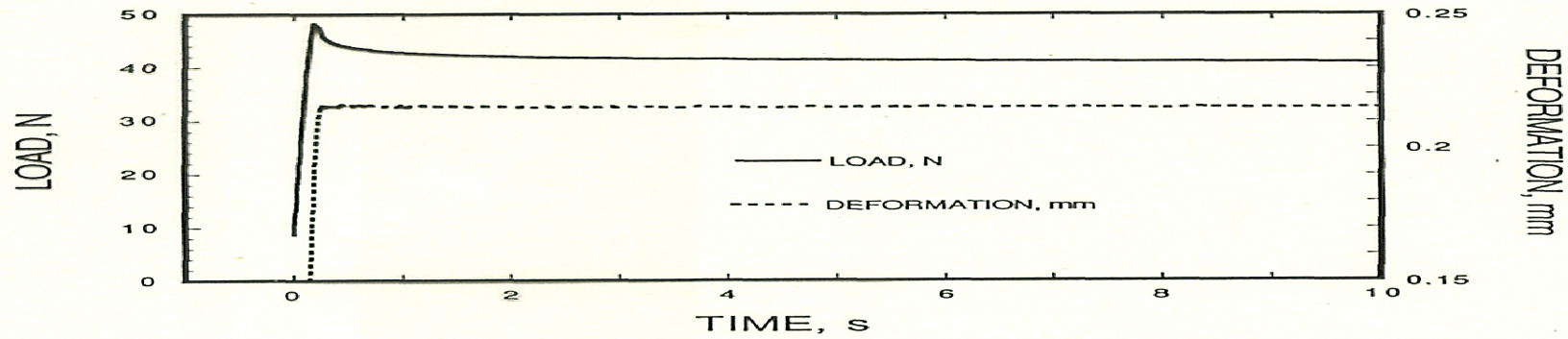


For rocks, load relaxation test has to be carried out under sufficiently large initial displacement. Sub-critical crack can easily be arrested or locked at barriers, or asperities.

After Pletka et al. (1979).

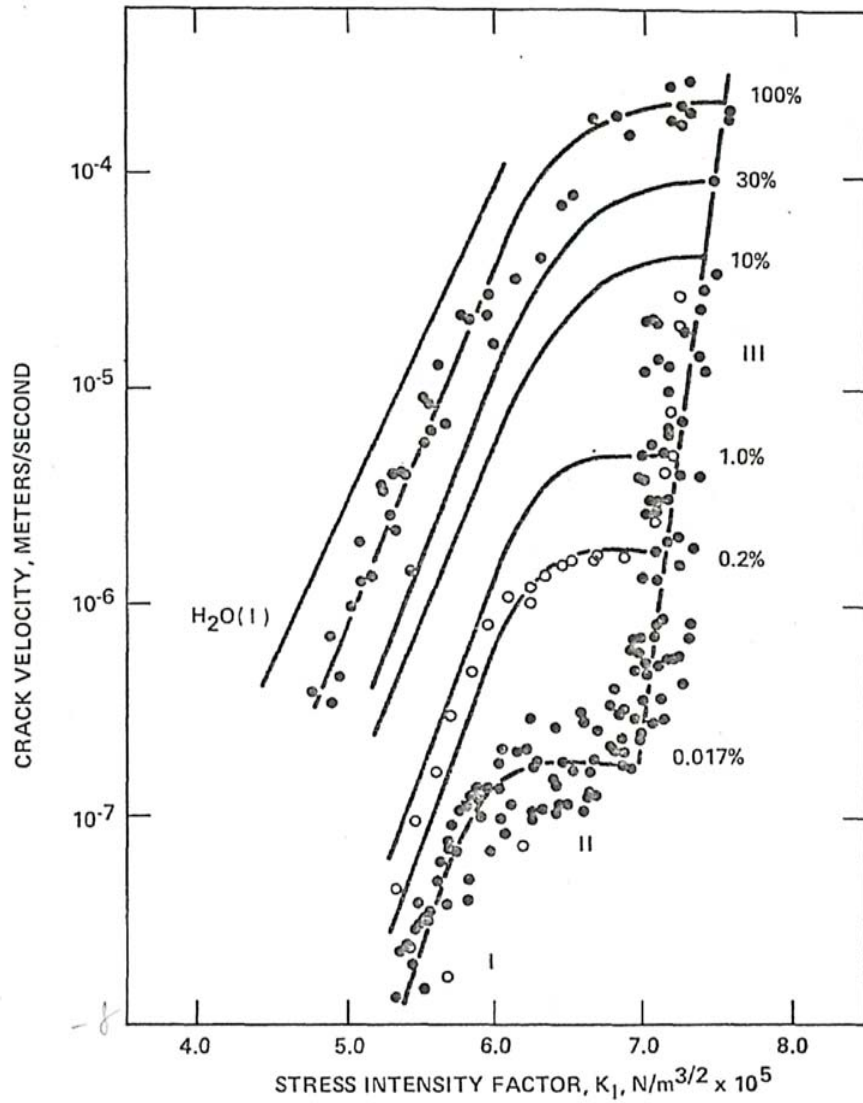




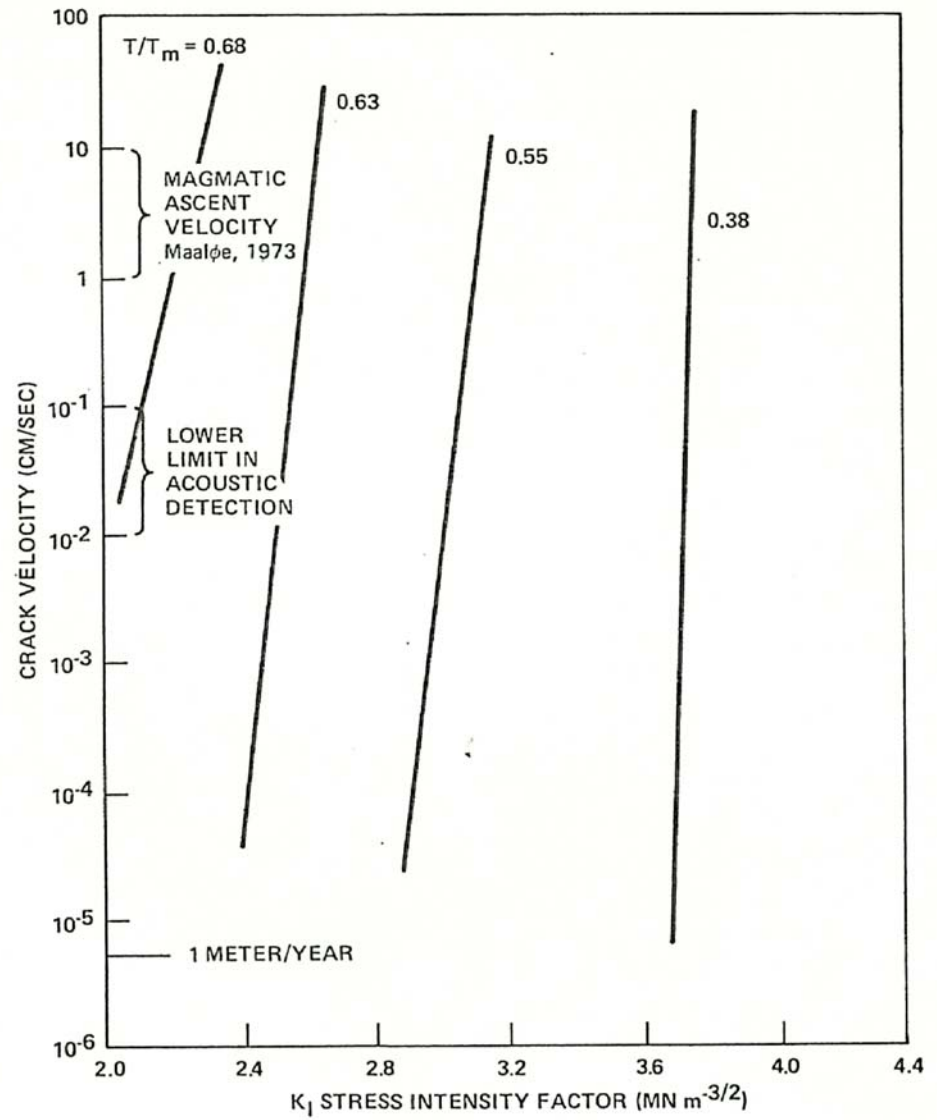


Memo: regarding to seismic effects on crack velocity, see Kerkhof, F., Proc. Int. Conf. Dynamic Crack Propagation, ed. Sih, Noordhoff Int. Publ., Leyden, 3-35, 1972.

We have to consider High temperature, high pressure and water.



After Wiederhorn (1967).



After Anderson and Grew (1979).